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Estimating the cross-sectional distribution of price stickiness from aggregate data

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### Resumé

Vi estimerer en multi-sektor-model med stive priser for den amerikanske økonomi, hvor graden af prisstivhed kan variere mellem sektorerne. Til dette formål opstiller vi en modelramme, der tillader os at udlede information fra makroøkonomiske tidsserier om den underliggende fordeling af prisstivhed på tværs af sektorerne. Identifikationen er mulig, idet effekten af økonomiske chok på makroøkonomiske variable via prisdannelsen varierer mellem sektorerne: Sektorer med udtalt prisstivhed fører således til en mere lavfrekvent påvirkning af chok på de makroøkonomiske variable.

Når modellen estimeres alene på makroøkonomiske variable for nominelt og realt BNP, opnår vi en estimeret fordeling af prisstivhed på tværs af økonomien, som stemmer godt overens med den empiriske fordeling, man kan konstruere fra mikroøkonomiske studier af prisdannelsen i USA. Vi estimerer også fordelinger for prisstivheden i ti andre lande, inkl. Danmark. Endelig udnytter vi vor bayesianske tilgang til at kombinere de makroøkonomiske tidsserier med informationen om prisstivhed fra de mikroøkonomiske studier i en integreret estimationsalgoritme.

Vore resultater viser, at det er af afgørende betydning at tage højde for heterogeniteten i prisstivheder på tværs af økonomien, når man analyserer den dynamiske sammenhæng mellem produktion og prisdannelse. Som sådan kan denne analyse ses som et skridt på vejen mod at forstå sammenhængen mellem den prisstivhed, der typisk estimeres på basis af makroøkonomiske tidsserier, og den, der udledes fra mikroøkonomiske observationer.

# Estimating the Cross-Sectional Distribution of Price Stickiness from Aggregate Data\*

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January, 2010

### Abstract

We estimate a multi-sector sticky-price model for the U.S. economy in which the degree of price stickiness is allowed to vary across sectors. For this purpose, we use a specification that allows us to extract information about the underlying cross-sectional distribution from aggregate data. Identification is possible because sectors play different roles in determining the response of aggregate variables to shocks at different frequencies: sectors where prices are more sticky are relatively more important in determining the low-frequency response. Estimating the model using only aggregate data on nominal and real output, we find that the inferred distribution of price stickiness is strikingly similar to the empirical distribution constructed from the recent microeconomic evidence on price setting in the U.S. economy. We also provide macro-based estimates of the underlying distribution for ten other countries. Finally, we explore our Bayesian approach to combine the aggregate time-series data with the microeconomic information on the distribution of price rigidity. Our results show that allowing for this type of heterogeneity is critically important to understanding the joint dynamics of output and prices, and it constitutes a step toward reconciling the extent of nominal price rigidity implied by aggregate data with the evidence from price micro data.

JEL classification codes: E10, E30

Keywords: heterogeneity, price stickiness, micro data, macro data, Bayesian estimation

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### 1 Introduction

Comparisons of estimates of important economic parameters based on microeconomic or disaggregated data versus those based on aggregate data often produce a conflicting picture. Perhaps the prime example involves estimates of the elasticity of individual labor supply, which are typically smaller than estimates of the elasticity of the aggregate labor supply. Other examples are the elasticity of substitution between domestic and foreign goods - which is substantially higher when estimated from disaggregated data, and the parameters determining the extent of habit formation in consumption - which may differ significantly depending on whether microeconomic or aggregate data are employed in the estimation. These discrepancies are usually associated with a large amount of heterogeneity in estimates of the parameters based on disaggregated data, which contrasts with the (explicit or implicit) homogeneity assumption that underlies most of the estimates based on aggregate data. These differences have fostered debates about how to calibrate models with representative agents, and also the development of heterogeneous-agents models that can reconcile the empirical findings.

Estimates of the extent of nominal price rigidity reveal the same kind of tension. A recent empirical literature that uses price micro data from various sources documents that, on average, prices change at least once a year (for a recent survey, see Klenow and Malin 2009). In contrast, estimates of the frequency of price changes from dynamic stochastic general equilibrium (DSGE) models and aggregate data point to much less frequent adjustment.<sup>4</sup> Likewise, evidence on the response of the aggregate price level to various shocks in vector autoregressions (VARs) points to sluggish adjustment. This discrepancy between micro- and macro-based evidence on price stickiness has shaped many of the developments in the field of Monetary Economics since the emergence of so-called new Keynesian Economics in the 1980s.

In this paper we take a step toward reconciling the apparent disconnect between micro- and macro-based estimates of nominal price rigidity. Our approach is motivated by the microeconomic evidence of substantial heterogeneity in the degree of price rigidity across sectors emphasized by Bils and Klenow (2004) and subsequent papers, and by recent theoretical work showing that such heterogeneity matters for aggregate dynamics.<sup>5</sup> We estimate a multi-sector sticky-price model for the U.S. economy in which the degree of price stickiness is allowed to vary across sectors. Our specification allows us to extract information about the underlying cross-sectional

<sup>&</sup>lt;sup>1</sup>For a recent discussion of some of these contrasting empirical findings, see Shimer (2009).

<sup>&</sup>lt;sup>2</sup>See, respectively, Imbs and Mejean (2009) and Ravina (2007).

<sup>&</sup>lt;sup>3</sup>See, for example, Browning et al. (1999) and Chang and Kim (2006).

<sup>&</sup>lt;sup>4</sup>See, for example, the recent survey by Maćkowiak and Smets (2008).

<sup>&</sup>lt;sup>5</sup>See Carvalho (2006) for results in a multi-sector version of the new Keynesian model, Carvalho and Schwartzman (2008) for a large class of time-dependent sticky-price and sticky-information models, and Enomoto (2007) and Nakamura and Steinsson (2009) for similar results in multi-sector menu-cost economies.

distribution from aggregate data. Identification is made possible by the fact that in the models different sectors are relatively more important in determining the response of aggregate variables to shocks at different frequencies. In particular, sectors where prices are more sticky are relatively more important in determining the low-frequency response to shocks; and vice-versa for more-flexible-price sectors.

We first estimate the model using only aggregate data on nominal and real Gross Domestic Product (GDP). We find that the cross-sectional distribution of price stickiness inferred from the aggregate data is strikingly similar to the empirical distribution that we construct from the micro-level statistics reported by Nakamura and Steinsson (2008) for 272 categories of goods and services of the Consumer Price Index. We also provide macro-based estimates of the underlying distribution for ten other countries, and show that the results line up well with the available microeconomic information.

We then explore our Bayesian estimation approach to combine the aggregate time-series data with the microeconomic information contained in the empirical cross-sectional distribution of price rigidity. We parameterize our prior over the set of parameters that characterize the cross-sectional distribution in the model in a way that easily allows us to relate its moments to moments of the empirical distribution. Estimation still relies only on aggregate data on nominal and real output as observables. We also estimate versions of the model that impose the same degree of price rigidity for all firms in the economy. The results discriminate sharply between the models with heterogeneity in price stickiness and their homogeneous-firms counterparts, and provide strong support for this type of heterogeneity. In a comparison with the best-fitting homogeneous model, the posterior odds in favor of the heterogeneous models is of the order of 10<sup>11</sup>: 1. Moreover, the homogeneous specification favored by the data implies an extent of price rigidity that, at 7 quarters, seems unrealistic in light of the microeconomic evidence. These results show that allowing for this type of heterogeneity is of critical importance for understanding the joint dynamics of output and prices, and constitutes an important step toward reconciling the extent of nominal price rigidity implied by aggregate data with the evidence from price micro data.

Until recently, most of the efforts devoted to reconciling micro- and macro-based evidence on price rigidity focused on mechanisms that can slow down the adjustment of the aggregate price level to shocks, in the context of models in which all prices are equally sticky. These mechanisms are usually referred to as "real rigidities" (a term due to Ball and Romer 1990): as long as price changes are not perfectly synchronized, such rigidities make it optimal for firms to undertake only a partial adjustment to shocks that affect the aggregate price level, whenever they do adjust. This is due to an interdependence in pricing decisions that is often referred to as a "strategic complementarity" in price setting.

For a given frequency of price adjustments, a model with heterogeneity in price stickiness can produce longer-lived aggregate dynamics than an otherwise identical homogeneous-firms model, even in the absence of pricing complementarities (Carvalho 2006, Carvalho and Schwatzman 2008). Yet, the two mechanisms can, and do coexist in our estimated model, helping it produce empirically more realistic aggregate dynamics. The reason is that our estimated parameters imply strategic complementarity in price setting. Coupled with heterogeneity in price rigidity, this leads firms in the more sticky sectors to become disproportionately important in shaping aggregate dynamics, through their influence on pricing decisions of firms that change prices more frequently.<sup>6</sup> This enhances the ability of the estimated model to deliver a cross-sectional distribution of price stickiness that accords well with the microeconomic evidence on price rigidity, and at the same time fit the data better than a homogeneous-firms model that features significantly more price stickiness.

The structure of the supply side of our model is a multi-sector economy with Taylor (1979, 1980) staggered price setting, in which the extent of price rigidity varies across different sectors. Instead of postulating a fully-specified economy to obtain the remaining equations to be used in the estimation, we assume exogenous stochastic processes for nominal output and for an unobservable natural rate of output; hence, we refer to our model as "semi-structural". Given that our focus is on estimation of parameters that characterize price-setting behavior in the economy in the presence of heterogeneity, our goal in specifying such exogenous time-series processes is to close the model with a set of equations that can provide it with some flexibility relative to a fully-structural model. This approach allows us to avoid having to find a demand-side specification that performs well empirically, which typically requires the introduction of various "frictions" that would move us away from the focus of our paper.

Our work is obviously related to the literature that emphasizes the importance of heterogeneity in price rigidity for aggregate dynamics. For brevity, and given our empirical focus, we refer the reader to Carvalho and Schwartzman (2008) for references to theoretical contributions. On the empirical front, Imbs et al. (2007) study the aggregation of sectoral Phillips curves, and the statistical biases that can arise from using estimation methods that do not account for heterogeneity. Their estimators that allow for heterogeneity produce results that are more in line with the available microeconomic evidence on price rigidity. Lee (2009) and Bouakez et al. (2008) estimate multi-sector DSGE models with heterogeneity in price rigidity using aggregate and sectoral data. They also find results that are more in line with the microeconomic picture than the

<sup>&</sup>lt;sup>6</sup>This potential amplification mechanism arising from the interaction between heterogeneity in price rigidity and pricing complementarities is discussed in detail in Carvalho (2006) and Carvalho and Schwartzman (2008).

<sup>&</sup>lt;sup>7</sup>Several earlier papers combine structural equations with empirical specifications for other parts of the model. Sbordone (2002), Guerrieri (2006) and Coenen et al. (2007) are recent examples.

versions of their models that impose the same degree of price rigidity for all sectors. Taylor (1993) provides estimates of the distribution of the durations of wage contracts in various countries inferred from aggregate data, while Guerrieri (2006) provides estimates of the distribution of the duration of price spells in the U.S. based on aggregate data. Both assume ex-post rather than ex-ante heterogeneity in nominal rigidities. Coenen et al. (2007) estimate a model with (limited) ex-ante heterogeneity in price contracts using only aggregate data. They focus on the estimate of the index of real rigidities and on the average duration of contracts implied by their estimates, which they emphasize is in line with the results in Bils and Klenow (2004). Jadresic (1999) is a precursor to some of the ideas in this paper. He estimates a model with ex-ante heterogeneous price spells using aggregate data for the U.S. economy to study the joint dynamics of output and inflation. Similarly to our findings, his statistical results reject the assumption of identical firms. Moreover, he discusses the intuition behind the mechanism that allows for identification of the cross-sectional distribution of price rigidity from aggregate data in his model, which is essentially the same as in our model.

In Section 2 we present the semi-structural model and study the extent to which aggregate data contain information about the cross-sectional distribution of price stickiness. Section 3 describes our empirical methodology. We detail the aggregate data used in the estimation, as well as our method for incorporating the information from the micro price data in our priors. This section also presents our prior assumptions, and Bayesian estimation algorithm. In Section 4 we present our results for the U.S. economy. We analyze the findings under informative and uninformative priors, and compare these with homogeneous-firms specifications. Section 5 presents macro-based estimates of price rigidity for ten other countries. We discuss robustness issues and directions for future research in Section 6, before concluding.

# 2 The semi-structural model

There is a continuum of monopolistically competitive firms divided into K sectors that differ in the frequency of price changes. Firms are indexed by their sector,  $k \in \{1, ..., K\}$ , and by  $j \in [0, 1]$ . The distribution of firms across sectors is summarized by a vector  $(\omega_1, ..., \omega_K)$  with  $\omega_k > 0$ ,  $\sum_{k=1}^K \omega_k = 1$ , where  $\omega_k$  gives the mass of firms in sector k. Each firm produces a unique variety of a consumption good, and faces a demand that depends negatively on its relative price.

In any given period, profits of firm j from sector k (henceforth referred to as "firm kj") are

 $<sup>^{8}</sup>$  This makes their frameworks closer to the generalized time-dependent model of Dotsey et al. (1997) than to our models with ex-ante heterogeneity.

<sup>&</sup>lt;sup>9</sup>Their model assumes indexation to either past inflation or a constant inflation objective. Thus, strictly speaking their finding is that the average time between contract reoptimizations is comparable to the average duration of price spells documented by Bils and Klenow (2004).

given by:

$$\Pi_{t}(k,j) = P_{t}(k,j) Y_{t}(k,j) - C(Y_{t}(k,j), Y_{t}, \xi_{t}),$$

where  $P_t(k,j)$  is the price charged by the firm,  $Y_t(k,j)$  is the quantity that it sells at the posted price (determined by demand), and  $C(Y_t(k,j), Y_t, \xi_t)$  is the total cost of producing such quantity, which may also depend on aggregate output  $Y_t$ , and is subject to shocks  $(\xi_t)$ . We assume that the demand faced by the firm depends on its relative price  $\frac{P_t(k,j)}{P_t}$ , where  $P_t$  is the aggregate price level in the economy, and on aggregate output. Thus, we write firm kj's profit as:

$$\Pi_{t}(k,j) = \Pi\left(P_{t}(k,j), P_{t}, Y_{t}, \xi_{t}\right),\,$$

and make the usual assumption that  $\Pi$  is homogeneous of degree one in the first two arguments, and single-peaked at a strictly positive level of  $P_t(k,j)$  for any level of the other arguments.<sup>10</sup>

The aggregate price index combines sectoral price indices,  $P_t(k)$ 's, according to the sectoral weights,  $\omega_k$ 's:

$$P_{t} = \Gamma\left(\left\{P_{t}\left(k\right), \omega_{k}\right\}_{k=1,\dots,K}\right),\,$$

where  $\Gamma$  is an aggregator that is homogeneous of degree one in the  $P_t(k)$ 's. In turn, the sectoral price indices are obtained by applying a symmetric, homogeneous-of-degree-one aggregator  $\Lambda$  to prices charged by all firms in each sector:

$$P_t(k) = \Lambda \left( \{ P_t(k,j) \}_{j \in [0,1]} \right).$$

We assume the specification of staggered price setting inspired by Taylor (1979, 1980). Firms set prices that remain in place for a fixed number of periods. The latter is sector-specific, and we save on notation by assuming that firms in sector k set prices for k periods. Thus,  $\omega = (\omega_1, ..., \omega_K)$  fully characterizes the cross-sectional distribution of price stickiness that we are interested in. Finally, across all sectors, adjustments are staggered uniformly over time.

When setting its price  $X_t(k,j)$  at time t, given that it sets prices for k periods, firm kj solves:

$$\max E_{t} \sum_{i=0}^{k-1} Q_{t,t+i} \Pi \left( X_{t} \left( k,j \right), P_{t+i}, Y_{t+i}, \xi_{t+i} \right),$$

where  $Q_{t,t+i}$  is a (possibly stochastic) nominal discount factor. The first-order condition for the

<sup>&</sup>lt;sup>10</sup>This is analogous to Assumption 3.1 in Woodford (2003).

firm's problem can be written as:

$$E_{t} \sum_{i=0}^{k-1} Q_{t,t+i} \frac{\partial \Pi \left( X_{t} \left( k,j \right), P_{t+i}, Y_{t+i}, \xi_{t+i} \right)}{\partial X_{t} \left( k,j \right)} = 0. \tag{1}$$

Note that all firms from sector k that adjust prices at the same time choose a common price, which we denote  $X_t(k)$ .<sup>11</sup> Thus, for a firm kj that adjusts at time t and sets  $X_t(k)$ , the prices charged from t to t + k - 1 satisfy:

$$P_{t+k-1}(k,j) = P_{t+k-2}(k,j) = \dots = P_t(k,j) = X_t(k)$$
.

Given the assumptions on price setting, and uniform staggering of price adjustments, with an abuse of notation sectoral prices can be expressed as:

$$P_{t}(k) = \Lambda \left( \{X_{t-i}(k)\}_{i=0,\dots,k-1} \right).$$

We close the model by specifying a stochastic process for the shock  $\xi_t$ , and by positing that nominal output  $M_t \equiv P_t Y_t$  also evolves in an exogenous fashion. This is a standard assumption in theoretical work on price setting (e.g. Mankiw and Reis 2002, or Woodford 2003, chapter 3). It allows us to focus on the implications of our particular model of price setting for the dynamics of aggregate output and prices without having to specify a full model of the economy.

### 2.1 A loglinear approximation

We assume that the economy has a deterministic zero-inflation steady state characterized by  $M_t = \overline{M}, \xi_t = \overline{\xi}, Y_t = \overline{Y}, Q_{t,t+i} = \beta^i$ , and for all  $(k,j), X_t(k,j) = P_t = \overline{P}$ , and loglinearize (1) around it to obtain:<sup>12</sup>

$$x_{t}(k) = \frac{1-\beta}{1-\beta^{k}} E_{t} \sum_{i=0}^{k-1} \beta^{i} \left( p_{t+i} + \zeta \left( y_{t+i} - y_{t+i}^{n} \right) \right),$$
 (2)

where lowercase variables denote log-deviations of the respective uppercase variables from the steady state. The parameter  $\zeta > 0$  is the Ball and Romer (1990) index of real rigidities. The new variable  $Y_t^n$  is defined implicitly as a function of  $\xi_t$  by:

$$\left. \frac{\partial \Pi \left( X_t \left( k, j \right), P_t, Y_t^n, \xi_t \right)}{\partial X_t \left( k, j \right)} \right|_{X_t \left( k, j \right) = P_t} = 0.$$

<sup>&</sup>lt;sup>11</sup>To a first-order approximation, adding firm-level heterogeneity in the form of idiosyncratic shocks that induce a non-degenerate distribution of prices among adjusting firms does not change any of the results, as long as these shocks cancel out when averaged over a continuum of firms.

<sup>&</sup>lt;sup>12</sup>We write all such approximations as equalities, ignoring higher-order terms.

In the loglinear approximation,  $y_t^n$  moves proportionately to  $\log (\xi_t/\overline{\xi})$ . Strictly speaking, it is the level of output that would prevail in a flexible-price economy. In a fully-specified model this would tie it down to preference and technological shocks. Here we do not pursue a structural interpretation of the exogenous processes driving the economy.<sup>13</sup> Nevertheless, for ease of presentation we follow the literature and refer to  $y_t^n$  as the "natural level of output."

The definition of nominal output yields:

$$m_t = p_t + y_t. (3)$$

Finally, we postulate that the aggregators that define the overall level of prices  $P_t$  and the sectoral price indices give rise to the following loglinear approximations:<sup>14</sup>

$$p_t = \sum_{k=1}^K \omega_k p_t(k), \qquad (4)$$

$$p_t(k) = \int_0^1 p_t(k,j) \, dj = \frac{1}{k} \sum_{j=0}^{k-1} x_{t-j}(k) \,. \tag{5}$$

Large real rigidities (small  $\zeta$  in equation (2)) reduce the sensitivity of prices to aggregate demand conditions, and thus magnify the non-neutralities generated by nominal price rigidity. In fully-specified models, the extent of real rigidities depends on primitive parameters such as the intertemporal elasticity of substitution, the elasticity of substitution between varieties of the consumption good, the labor supply elasticity. It also depends on whether the economy features economy-wide or segmented factor markets, whether there is an explicit input-output structure etc.<sup>15</sup> In the context of our model,  $\zeta$  is itself a primitive parameter. Following standard practice in the literature, we refer to economies with  $\zeta < 1$  as ones displaying strategic complementarities in price setting. To clarify the meaning of this expression, replace (3) in (2) to obtain:

$$x_{t}(k) = \frac{1-\beta}{1-\beta^{k}} E_{t} \sum_{i=0}^{k-1} \beta^{i} \left( \zeta \left( m_{t+i} - y_{t+i}^{n} \right) + (1-\zeta) p_{t+i} \right).$$
 (6)

That is, new prices are set as a discounted weighted average of current and expected future driving variables  $(m_{t+i} - y_{t+i}^n)$  and prices  $p_{t+i}$ .  $\zeta < 1$  implies that firms choose to set higher prices if the overall level of current and expected future prices is higher, all else equal. On the other hand,  $\zeta > 1$  means that prices are *strategic substitutes*, in that under those same circumstances

<sup>&</sup>lt;sup>13</sup>We think such an interpretation is unreasonable because we take nominal output to be exogenous. In that context, an interpretation of  $y_t^n$  as being driven by preference and technology shocks would imply that these shocks have no effect on nominal output (i.e. that they have exactly-offsetting effects on aggregate output and prices).

<sup>&</sup>lt;sup>14</sup>This is what comes out of a fully-specified multi-sector model with the usual assumption of Dixit-Stiglitz preferences.

<sup>&</sup>lt;sup>15</sup>For a detailed discussion of sources of real rigidities see Woodford (2003, chapter 3).

adjusting firms choose relatively *lower* prices.

# **2.2** Nominal $(m_t)$ and natural $(y_t^n)$ output

We postulate an  $AR(p_1)$  process for nominal output,  $m_t$ :

$$m_t = \rho_0 + \rho_1 m_{t-1} + \dots + \rho_{n_1} m_{t-n_1} + \varepsilon_t^m, \tag{7}$$

and an  $AR(p_2)$  process for the natural output level,  $y_t^n$ :

$$y_t^n = \delta_0 + \delta_1 y_{t-1}^n + \dots + \delta_{p_2} y_{t-p_2}^n + \varepsilon_t^n,$$
(8)

where 
$$\varepsilon_t = (\varepsilon_t^m, \varepsilon_t^n)$$
 is i.i.d.  $N\left(0_{1\times 2}, \Omega^2\right)$ , with  $\Omega^2 = \begin{bmatrix} \sigma_m^2 & 0\\ 0 & \sigma_n^2 \end{bmatrix}$ .

### 2.3 State-space representation and likelihood function

We solve the semi-structural model (2)-(8) with Gensys (Sims, 2002), to obtain:

$$Z_{t} = \mathcal{C}(\theta) + G_{1}(\theta) Z_{t-1} + B(\theta) \varepsilon_{t}. \tag{9}$$

where  $Z_t$  is a vector collecting all variables and additional "dummy" variables created to account for leads and lags and  $\varepsilon_t$  is as defined before. The vector  $\theta$  collects the primitive parameters of the model:

$$\theta = (K, p_1, p_2, \beta, \zeta, \sigma_m, \sigma_n, \omega_1, \cdots, \omega_K, \rho_0, \cdots, \rho_{p_1}, \delta_0, \cdots, \delta_{p_2}).$$

In all estimations that follow we make use of the likelihood function  $\mathcal{L}(\theta|Z^*)$ , where  $Z^*$  is the vector of observed time series (i.e. a subset of Z). Given that our state vector  $Z_t$  includes many unobserved variables, such as the natural output level and sectoral prices, the likelihood function is constructed through application of the Kalman filter to the solved loglinear model (9). Letting H denote the matrix that singles out the observed subspace  $Z_t^*$  of the state vector  $Z_t$  (i.e.,  $Z_t^* = HZ_t$ ), our distributional assumptions can be summarized as:

$$Z_{t}|Z_{t-1} \sim N\left(C\left(\theta\right) + G_{1}\left(\theta\right)Z_{t-1}, B\left(\theta\right)\Omega B\left(\theta\right)'\right),$$

$$Z_{t}^{*}|\left\{Z_{\tau}^{*}\right\}_{\tau=1}^{t-1} \sim N\left(\mathcal{M}_{t|t-1}\left(\theta\right), V_{t|t-1}\left(\theta\right)\right),$$

where  $\mathcal{M}_{t|t-1}(\theta) \equiv HC(\theta) + HG_1(\theta) \hat{Z}_{t|t-1}$ ,  $V_{t|t-1}(\theta) \equiv HB(\theta) \hat{\Sigma}_{t|t-1}B(\theta)'H'$ ,  $\hat{Z}_{t|t-1}$  denotes the expected value of  $Z_t$  given  $\{Z_{\tau}^*\}_{\tau=1}^{t-1}$ , and  $\hat{\Sigma}_{t|t-1}$  is the associated forecast-error covariance matrix.

### 2.4 Identification of the cross-sectional distribution from aggregate data

In estimating our multi-sector model we only use data on aggregate nominal and real output as observables. It is thus natural to ask whether the structure of the model is such that these aggregate data reveal information about the cross-sectional distribution of price stickiness  $\omega = (\omega_1, ..., \omega_K)$ . As in Jadresic (1999), we start by looking at a simple case where it is easy to show that  $\omega$  can be inferred from observations of those two aggregate time series. This helps develop the intuition for a more general case for which we can also show identification. We then assess the small-sample properties of estimates of  $\omega$  inferred from aggregate data through a Monte Carlo exercise. As in our estimation, we assume throughout that the discount factor,  $\beta$ , is known.

The key simplifying assumption to show identification in the first case is absence of pricing interactions:  $\zeta = 1$ . In that case, from (6) new prices  $x_t(k)$  are set on the basis of current and expected future values of the two exogenous processes  $m_t$  and  $y_t^n$ . For simplicity and without loss of generality, assume further that the latter follow the AR(1) processes:

$$m_t = \rho_1 m_{t-1} + \varepsilon_t^m$$
, and (10)

$$y_t^n = \delta_1 y_{t-1}^n + \varepsilon_t^n. \tag{11}$$

Then new prices are set according to:

$$x_t(k) = F(\beta, \rho_1, k) m_t - F(\beta, \delta_1, k) y_t^n$$

where

$$F(\beta, a, k) \equiv \left(1 + \frac{1 - \beta}{1 - \beta^k} \frac{\beta a - (\beta a)^k}{1 - \beta a}\right).$$

Replacing this expression for newly set prices in the sectoral price equation (5) and aggregating according to (4) produces the following expression for the aggregate price level:

$$p_{t} = \sum_{j=0}^{K-1} \sum_{k=j+1}^{K} F(\beta, \rho_{1}, k) \frac{\omega_{k}}{k} m_{t-j} - \sum_{j=0}^{K-1} \sum_{k=j+1}^{K} F(\beta, \delta_{1}, k) \frac{\omega_{k}}{k} y_{t-j}^{n}.$$
(12)

If we observe  $m_t$  and  $y_t$  - and thus  $p_t$ , estimates of the coefficients on  $m_{t-j}$  in (12) allow us to infer the sectoral weights  $\omega$ . The reason is that  $F(\beta, \rho_1, k)$  is "known", since  $\rho_1$  can be estimated directly from (10). Thus, knowledge of the coefficient on the longest lag of  $m_{t-j}$  (attained when j = K - 1) allows us to uncover  $\omega_K$ . The coefficient on the next longest lag  $(m_{t-(K-2)})$  depends on  $\omega_{K-1}$  and  $\omega_K$ , which reveals  $\omega_{K-1}$ . We can thus recursively infer the sectoral weights from the coefficients  $F(\beta, \rho_1, k) \frac{\omega_k}{k}$ . Moreover, identification obtains with any estimation method that

produces consistent estimates of these coefficients. 16

Checking for identification of  $\omega$  in the presence of pricing interactions ( $\zeta \neq 1$ ) is more difficult. To gain intuition on why this is so, fix the case of pricing complementarities ( $\zeta < 1$ ). Then, because of the delayed response of sticky-price firms to shocks, firms with flexible prices will only react partially to innovations to  $m_t$  and  $y_t^n$  on impact. They will eventually react fully to the shocks, but also with a delay. This illustrates why the clean recursive identification that applies when  $\zeta = 1$  no longer works. It turns out that in equilibrium these pricing interactions manifest themselves through a dependence of the aggregate price level on its own lags. Knowledge of the coefficients on these lags and on lagged nominal output again allows us to solve for the sectoral weights (and for  $\zeta$ ). In practice, however, the analytical exercise involves extremely long mathematical expressions and, except for models with a small number of sectors, is all but infeasible. For that reason, and also for brevity, in the Appendix we illustrate how the process works in a two-sector model.

The intuition behind the identification result in the absence of pricing interactions is clear: the impact of older developments of the exogenous processes on the current price level depends on prices that are sticky enough to have been set when the shocks hit. This provides information on the share of the sector with that given duration of price spells (and sectors with longer durations). More generally, in the presence of pricing interactions current fully-forward-looking pricing decisions may also reflect past developments of the exogenous processes. The intuition behind the mechanism that allows for identification extends in a natural way: sectors where prices are more sticky are relatively more important in determining the impact of older shocks to the exogenous processes on the current price level, and vice-versa for more-flexible-price sectors.

These results on identification are of little use to us if the mechanism highlighted above does not work well in practice. We now turn to a Monte Carlo exercise to verify whether or not this is the case. We generate artificial data on aggregate nominal and real output using a model with K=4, and parameter values that roughly resemble what we find when we estimate a model of this size on actual U.S. data. Then, we estimate the parameters of the model by maximum likelihood.<sup>17</sup> We conduct both a large- (1000 observations) and a small-sample exercise (100 observations, as in our actual sample).

Table 1 reports the true parameter values used to generate the data in the first column. The columns under "Large sample" report statistics across 75 artificial samples of 1000 observations

<sup>&</sup>lt;sup>17</sup>We apply the same procedure that we use in the initial maximization stage of the Markov Chain Monte Carlo algorithm that we use to estimate the models with actual data, including the choice of initial values for the optimization algorithm (see Subsection 3.4).

each. The "Small sample" columns report statistics across 240 artificial samples of 100 observations each.<sup>18</sup> The "Ini. guess" column reports the average value of the initial guesses supplied for the optimization algorithm across the corresponding samples.

Table 1: Monte Carlo - maximum likelihood estimation

			Larg	ge sample			Sma	ll sample	
	True	Mean	$5^{th}$ perc.	$95^{th}$ perc.	Ini. guess	Mean	$5^{th}$ perc.	$95^{th}$ perc.	$Ini.\ guess$
ζ	0.10	0.106	0.059	0.15	1.00	0.179	0.022	0.415	1.00
$\omega_1$	0.40	0.395	0.183	0.621	0.25	0.318	0.033	0.871	0.25
$\omega_2$	0.10	0.100	0.000	0.257	0.25	0.096	0.000	0.376	0.25
$\omega_3$	0.10	0.091	0.000	0.197	0.25	0.088	0.000	0.304	0.25
$\omega_4$	0.40	0.414	0.233	0.570	0.25	0.498	0.064	0.801	0.25
$ ho_0$	0.00	0.000	0.000	0.000	0.000	0.000	-0.002	0.002	0.000
$ ho_1$	1.43	1.432	1.388	1.468	1.429	1.403	1.256	1.547	1.538
$ ho_2$	-0.45	-0.456	-0.499	-0.410	-0.455	-0.446	-0.579	-0.302	-0.577
$\sigma_m$	0.005	0.005	0.0048	0.0051	0.005	0.005	0.0043	0.0056	0.0058
$\delta_0$	0.00	0.000	-0.001	0.001	0.000	0.000	-0.004	0.004	0.000
$\delta_1$	0.35	0.336	0.091	0.513	1.066	0.231	-0.257	0.616	0.954
$\delta_2$	0.15	0.146	0.049	0.258	-0.199	0.133	-0.073	0.326	-0.076
$\sigma_n$	0.05	0.053	0.033	0.083	0.0067	0.105	0.020	0.311	0.0062

Note: The columns under "Large sample" report statistics across 75 artificial samples of 1000 observations. The "Small sample" columns report statistics across 240 artificial samples of 100 observations. The "Ini. guess" column reports the average value of the initial guesses across the corresponding samples. Following the procedure that we use in the actual estimation algorithm, the initial guesses for  $\zeta$  and  $\omega_1 - \omega_4$  are the same across replications; the guesses for the remaining parameters in each replication are set equal to the ordinary least squares estimates based on nominal output (for the  $\rho$ 's) and actual output (for the  $\delta$ 's).

For the large samples, the estimates are quite close to the true parameter values, and fall within a relatively narrow range. For samples of the same size as our actual sample, we also find the aggregate data to be informative of the distribution of sectoral weights. However, in this case the estimates are moderately biased and somewhat less precise. This finding underscores our case for incorporating information from the microeconomic evidence on price-setting, as we do in our second estimation of the model.

# 3 Empirical methodology and data

With the challenges involved in bridging the gap between microeconomic information on firms' pricing behavior and time series of aggregate nominal and real output, the choice of empirical methodology is of critical importance. We employ a Bayesian approach as this allows us to

<sup>&</sup>lt;sup>18</sup>In each replication, the sample contains an additional 16 observations that we use as a pre-sample to initialize the Kalman filter, as we do in the actual estimation. The value of  $\beta$  is fixed at 0.99.

eventually integrate microeconomic information on the distribution of price rigidity with those macroeconomic time series. With some abuse of notation, the Bayesian principle can be shortly stated as:

$$f(\theta|Z^*) = f(Z^*|\theta) f(\theta) / f(Z^*) \propto \mathcal{L}(\theta|Z^*) f(\theta),$$

where f denotes density functions,  $Z^*$  is the vector of observed time series defined previously,  $\theta$  is the vector of primitive parameters, and  $\mathcal{L}(\theta|Z^*)$  is the likelihood function.

We use our sources of information in two complementary ways. First, we estimate the cross-sectional distribution of price stickiness using time-series data on aggregate nominal and real output under a prior distribution that is "flat" (uninformative) over the vector of sectoral weights. The macro-based estimates are then compared with the recent microeconomic evidence on price rigidity in the U.S. documented by Nakamura and Steinsson (2008).<sup>19</sup> In a second estimation we incorporate the information from the microeconomic data for the U.S. through a prior on the cross-sectional distribution of price stickiness, and estimate the model using the same set of observables. In the next subsection we detail how we use the microeconomic information from Nakamura and Steinsson (2008).

We also estimate the same model on the corresponding data for ten other countries, and provide an assessment of our macro-based estimates in light of the available (but in most cases much more limited) microeconomic evidence. The countries are Australia, Canada, Denmark, France, Italy, Korea, Norway, Sweden, Switzerland, and the United Kingdom (U.K.).<sup>20</sup>

### 3.1 Empirical distribution of price stickiness and prior over $\omega$

We extract our microeconomic information about the cross-sectional distribution of price stickiness from Nakamura and Steinsson (2008). Following the seminal work of Bils and Klenow (2004), they analyze the frequency of price changes in the U.S. economy using quite disaggregated datasets from the Bureau of Labor Statistics, which underlie the construction of price indices. We work with the statistics on the frequency of regular price changes (i.e. excluding those associated with sales and product substitutions) that they report for 272 categories of goods and services contained in the Consumer Price Index.

<sup>&</sup>lt;sup>19</sup>In a previous version of the paper we also analyzed the results in light of the statistics reported by Bils and Klenow (2004). For models with few sectors and limited heterogeneity, we found that the distribution of price rigidity inferred from the aggregate data is more similar to the empirical distribution constructed from Bils and Klenow (2004) than to the one constructed from Nakamura and Steinsson (2008). For models with more sectors and (potentially) more heterogeneity the results accord better with the latter paper. Moreover, statistical model comparisons strongly favor the specifications that allow for more heterogeneity in price rigidity. For brevity we chose to report only the latter results. An earlier draft of the paper with many more results is available upon request.

<sup>&</sup>lt;sup>20</sup>These countries were chosen on the basis of availability of data on real GDP and GDP deflator in the OECD database for roughly the same time period used in the estimation for the U.S. economy. The only exception is Denmark, for which the quarterly data starting in 1979 was provided to us by the Danmarks Nationalbank.

Our goal is to map those statistics into an empirical distribution of sectoral weights over spells of price rigidity with different durations. We work at a quarterly frequency, and for computational reasons consider economies with at most 8 quarters of price stickiness. Sectors correspond to price spells which are multiples of one quarter. We aggregate the goods and services categories so that the ones which have an average implied duration of price spells between zero and one quarter (inclusive) are assigned to the first sector; the ones with an average duration between one (exclusive) and two quarters (inclusive) are assigned to the second sector, and so on. The sectoral weights are aggregated accordingly by adding up the corresponding CPI expenditure weights. We proceed in this fashion until the sector with 7-quarter price spells. Finally, we aggregate all the remaining categories, which have average implied durations of price rigidity of 8 quarters and beyond, into a sector with 2-year price spells. This gives rise to the empirical cross-sectional distribution of price stickiness that we use to either assess the results obtained under flat priors, or as information to be incorporated in the estimation. The distribution is summarized in Table 2. We denote the sectoral weight for sector k obtained from this procedure by  $\widehat{\omega}_k$ . We also compute the average duration of price spells,  $\hat{k} = \sum_{k=1}^K \hat{\omega}_k k$ , and the standard deviation of the underlying distribution,  $\hat{\sigma}_k = \sqrt{\sum_{k=1}^K \hat{\omega}_k \left(k - \hat{k}\right)^2}$ .

Table 2: Empirical cross-sectional distribution of price stickiness Parameter  $\widehat{\omega}_1$ 

Value 0.27 0.07 0.10 0.11 0.06 0.13 0.06 0.20 (\*) In quarters.  $\sum \widehat{\omega}_k$  might differ from unity due to rounding. 2.66

Around 27% of firms change prices every quarter or more often; 55% change prices at least once a year; 20% change prices less frequently than once every two years. The average duration of price spells is just shy of 13 months, and the (cross-sectional) standard deviation of the distribution of price spells is 8 months.

In our Bayesian estimations we specify priors over the set of sectoral weights  $\omega = (\omega_1, ..., \omega_K)$ , which are then combined with the priors on the remaining parameters to produce the joint prior distribution for the set of all parameters of interest. We impose the combined restrictions of non-negativity and summation to unity of the  $\omega$ 's through a Dirichlet distribution, which is a multivariate generalization of the beta distribution. Notationally,  $\omega \sim D\left(\alpha\right)$  with density function:

$$f_{\omega}\left(\omega|\alpha\right) \propto \prod_{k=1}^{K} \omega_{k}^{\alpha_{k}-1}, \ \forall \alpha_{k} > 0, \ \forall \omega_{k} \geq 0, \ \sum_{k=1}^{K} \omega_{k} = 1.$$

The Dirichlet distribution is well known in Bayesian econometrics as the conjugate prior for the

multinomial distribution, and the hyperparameters  $\alpha_1, ..., \alpha_K$  are most easily understood in this context, where they can be interpreted as the number of occurrences for each of the K possible outcomes that the econometrician assigns to the prior information.<sup>21</sup> Thus, for given  $\alpha_1, ..., \alpha_K$ ,  $\alpha_0 \equiv \sum_k \alpha_k$  captures in some sense the overall level of information in the prior distribution. The information about the cross-sectional distribution of price stickiness comes from the relative sizes of the  $\alpha_k$ 's. The latter also determine the marginal distributions for the  $\omega_k$ 's. For example, the expected value of  $\omega_k$  is simply  $\alpha_k/\alpha_0$ , whereas its mode equals  $(\alpha_0 - K)^{-1}(\alpha_k - 1)$  (provided that  $\alpha_i > 1$  for all i).

We use the empirical cross-sectional distribution reported in Table 2 to pin down the relative values for the hyperparameters  $\alpha_1, ..., \alpha_K$ . We do this in a way that sets the mode of the prior distribution of sectoral weights equal to the empirical distribution. That requires setting  $\alpha_k = 1 + \widehat{\omega}_k (\alpha_0 - K)$ .

As mentioned previously, our first estimation does not make use of the microeconomic information, and imposes a "flat" prior in which all  $\omega$  vectors in the K-dimensional unit simplex are assigned equal prior density. This corresponds to  $\alpha_0 = K$ , and thus  $\alpha_k = 1$  for all k. This case allows us to assess the information that the aggregate data contain about the cross-sectional distribution of price stickiness. Subsequently, when we incorporate the microeconomic information in the estimation, we simply set  $\alpha_0 > 1$ , choosing the value to determine the tightness of the prior distribution around the empirical distribution of sectoral weights.

### 3.2 Priors on remaining parameters

The remaining model parameters fall into three categories that are dealt with in turn. Our goal in specifying their prior distributions is to avoid imposing any meaningful penalties on most parameter values - except for those that really seem extreme on an a priori basis. The first set comprises the  $\rho$ 's and  $\delta$ 's, parameterizing the exogenous AR processes for nominal and natural output, respectively. These are assigned loose Gaussian priors with mean zero. We choose to fix the lag length at two for both processes, i.e.  $p_1 = p_2 = 2$ . The second set of parameters consists of the standard deviations of the shocks to nominal  $(\sigma_m)$  and natural output  $(\sigma_n)$ . These are strictly positive parameters to which we assign loose Gamma priors. The last parameter is the Ball-Romer index of real rigidity,  $\zeta$ , which should also be non-negative. This is captured with a very loose Gamma prior distribution, with mode at unity and a 5-95 percentile interval equal

 $<sup>^{21}</sup>$ Gelman et al. (2003) offers a good introduction to the use of Dirichlet distribution as a prior distribution for the multinomial model.

 $<sup>^{22}</sup>$ In principle we could have specified priors over  $p_1$ ,  $p_2$  and estimated their posterior distributions as well. However, the computational cost of estimating all the models in the paper is already quite high, and we restrict ourselves to this specification with fixed number of lags. Our conclusions are robust to alternative assumptions about the number of lags (see Section 6).

to (0.47, 16.9). Hence, any significant degree of strategic complementarity or substitutability in price setting should be a result of the estimation rather than of our prior assumptions. These priors are summarized in Table  $3.^{23}$ 

Table 3: Prior distributions for remaining parameters

Parameter	Parameter Distribution		Mean	Std.dev.
ζ	$\operatorname{Gamma}(1.2, 0.2)$	1.00	6.00	5.48
$\sigma_n,\sigma_m$	$\operatorname{Gamma}(1.5,20)$	0.025	0.075	0.06
$\rho_j, \delta_j$	$N(0,5^2)$	0.00	0.00	5.00

Note: The hyper-parameters for the Gamma distribution specify shape and inverse scale, respectively, as in Gelman et al. (2003).

### 3.3 Macroeconomic time series

The model laid out is tested against the development of quarterly nominal and real output. These are measured as seasonally-adjusted GDP at, respectively, current and constant prices. We take natural logarithms and remove a linear trend from the data. Whereas the assumptions underlying the model include one of an unchanged economic environment, the U.S. economy has undergone profound changes in the recent decades, including the so-called "Great Moderation" and the Volcker Disinflation. As a consequence, we choose not to confront the model with the full sample of post-war data. We use the period from 1979 to 1982 as a pre-sample, and evaluate the model according to its ability to match business cycle developments in nominal and real output in the period 1983-2007.<sup>24</sup> Estimations for the other ten countries use the analogous data taken from the OECD database (http://stats.oecd.org). Data for Sweden are only available since 1980, and data for Italy are available since 1981. In these cases we shorten the pre-sample and start the actual sample in 1983Q1, as for the U.S. economy.

### 3.4 Simulating the posterior distribution

The joint posterior distribution of the model parameters is obtained through application of a Markov-chain Monte Carlo (MCMC) Metropolis algorithm. The algorithm produces a simulation sample of the parameter set that converges to the joint posterior distribution under certain conditions.<sup>25</sup> We provide details of our specific estimation process in the Appendix. The outcome

<sup>&</sup>lt;sup>23</sup>We do not include  $\beta$  in the estimation, and fix  $\beta = 0.99$ .

 $<sup>^{24}</sup>$ We make use of the pre-sample 1979-1982 by initializing the Kalman filter in the estimation stage with the estimate of  $Z_t$  and corresponding covariance matrix obtained from running a Kalman filter in the pre-sample. We use the parameter values in each draw. For the initial condition for the pre-sample, we use the unconditional mean and a large variance-covariance matrix.

<sup>&</sup>lt;sup>25</sup>These conditions are discussed in Gelman et al. (2003, part III).

is a sample of one million draws from the joint posterior distribution of the parameters of interest, based on which we draw the conclusions that we start to report in the next section.

Having obtained a sample of the posterior distribution of parameters from any given model, we can estimate the marginal posterior density (henceforth MPD) of the data given the model as:

$$MPD_{j} = f\left(Z^{*}|\mathcal{M}_{j}\right) = \int \mathcal{L}\left(\theta|Z^{*},\mathcal{M}_{j}\right) f\left(\theta|\mathcal{M}_{j}\right) d\theta,$$

and use it for model-comparison purposes. Here  $\mathcal{M}_j$  refers to a specific configuration of the model and prior distribution, and  $f(\theta|\mathcal{M}_j)$  denotes the corresponding joint prior distribution. Specifically, we approximate  $\log \text{MPD}_j$  for each model using Geweke's (1999) modified harmonic mean. We use these estimates to evaluate the empirical fit of the models relative to one another. The MPD ratio of two model configurations constitutes the *Bayes factor*, and – when neither configuration is a priori considered more likely – the posterior odds. It indicates how likely the two models are relative to one another given the observed data  $Z^*$ .

# 4 Results for the U.S. economy

# **4.1** Flat prior for $\omega$ ( $\alpha_0 = K$ )

Throughout the paper we restrict attention to multi-sector models with  $K=8.^{26}$  Table 4 and Figure 1 report the results in terms of marginal distributions for the parameters. The distribution that we infer from aggregate data is surprisingly similar to the empirical one (reproduced in the last column for ease of comparison). Using the posterior means as the point estimates for the sectoral weights - reported in the third column of numbers - approximately 28% of firms change prices every quarter; 43% change prices at least once a year; 13% change prices once every two years. The average duration of price spells is 13 months, and the standard deviation of the (cross-sectional) distribution of price spells is approximately 8 months. These numbers are quite close to the empirical distribution. The correlation between estimated and empirical sectoral weights is 0.62.

The index of real rigidities implies strong pricing complementarities. The posterior mean of  $\zeta$  is 0.05 and the 95<sup>th</sup> percentile equals 0.11, which falls within the 0.10-0.15 range that Woodford (2003) argues can be made consistent with fully-specified models.<sup>29</sup> As highlighted

<sup>&</sup>lt;sup>26</sup>In earlier versions of the paper we also estimated specifications with fewer sectors (see footnote 19).

<sup>&</sup>lt;sup>27</sup>We use a Gaussian kernel density estimator to graph the marginal posterior density for each parameter. The priors on  $\bar{k}$  and  $\sigma_k$  are based on 100,000 draws from the prior Dirichlet distribution.

<sup>&</sup>lt;sup>28</sup>Taking means of the marginal distributions as point estimates ensures that the weights sum to unity. This restriction is not necessarily satisfied by taking the posterior modes or medians of the marginal distributions. The results are almost insensitive to using alternative point estimates such as the values at the joint posterior mode, or taking medians or modes from the marginal ditributions and renormalizing so that the weights sum to unity.

<sup>&</sup>lt;sup>29</sup>This finding contrasts sharply with the results in Coenen et al. (2007). They rely on indirect-inference

Table 4: Parameter estimates for the U.S. economy - flat prior

	Model	with $K = 8$ , $\alpha_0 =$	: 8	$Empirical\\ distribution$
ζ	4.440 (0.466;16.863)	$\underset{(0.015;0.111)}{0.042}$	0.05	_
$\omega_1$	0.094 $(0.007; 0.348)$	0.264 $(0.099; 0.493)$	0.28	0.27
$\omega_2$	0.094 $(0.007; 0.348)$	0.072 $(0.007; 0.212)$	0.09	0.07
$\omega_3$	0.094 $(0.007; 0.348)$	0.020 $(0.002;0.078)$	0.03	0.10
$\omega_4$	0.094 $(0.007; 0.348)$	0.027 $(0.002;0.107)$	0.04	0.11
$\omega_5$	0.094 $(0.007; 0.348)$	0.144 $(0.017; 0.337)$	0.16	0.06
$\omega_6$	0.094 $(0.007; 0.348)$	0.123 $(0.011; 0.345)$	0.14	0.13
$\omega_7$	0.094 $(0.007; 0.348)$	0.120 $(0.010; 0.353)$	0.14	0.06
$\omega_8$	0.094 $(0.007; 0.348)$	$0.112 \\ (0.010; 0.323)$	0.13	0.20
$ar{k}$	4.501 (3.245;5.760)	4.394 (3.214;5.462)	4.37	4.25
$\sigma_k$	$\underset{(1.584; 2.678)}{2.139}$	$\begin{array}{c} 2.523 \\ (2.112; 2.893) \end{array}$	2.62	2.66
$ ho_0$	$0.000 \ (-8.224; 8.224)$	$\underset{(-0.001;0.001)}{0.000}$	0.000	_
$ ho_1$	$0.000 \\ (-8.224; 8.224)$	$\frac{1.426}{(1.273;1.576)}$	1.426	_
$\rho_2$	$0.000 \\ (-8.224; 8.224)$	-0.446 $(-0.593; -0.296)$	-0.446	_
$\sigma_m$	$0.059 \\ \scriptscriptstyle (0.009; 0.195)$	$0.005 \\ (0.005; 0.006)$	0.005	_
$\delta_0$	0.000 $(-8.224; 8.224)$	0.002 $(-0.002;0.007)$	0.003	_
$\delta_1$	$0.000 \\ (-8.224; 8.224)$	0.541 $(0.270;0.763)$	0.532	_
$\delta_2$	0.000 $(-8.224; 8.224)$	0.146 $(-0.027;0.331)$	0.149	_
$\sigma_n$	0.059 $(0.009;0.195)$	0.069 $(0.030;0.172)$	0.081	-

Note: The first two columns report the medians for, respectively, the marginal prior and posterior distributions; the third column gives the mean of the marginal posterior distribution; numbers in parentheses correspond to the  $5^{\rm th}$  and  $95^{\rm th}$  percentiles; the last column reproduces the empirical distribution from Table 2.

in Carvalho (2006), in this type of model these complementarities interact with heterogeneity in price stickiness to amplify the aggregate effects of nominal rigidities.

# 4.2 Combining micro and macro data in the estimation

We now use the available microeconomic information on the cross-sectional distribution of price stickiness in the estimation, through the prior distribution over  $\omega$ . As discussed in Subsection 3.1, we control the tightness of the prior by varying the parameter  $\alpha_0$ . Table 5 and Figure 2 present the results in terms of marginal distributions for the parameters assuming  $\alpha_0 = 80.30$ 

As expected, the posterior distributions for the sectoral weights now look more similar to the prior distributions. As an indication of the effect on the estimation of incorporating the microeconomic information, the correlation between estimated and empirical sectoral weights is now almost 0.98 (using the posterior means as the point estimates of the sectoral weights).

Incorporating the microeconomic information produces only small changes to the posterior distributions of the remaining parameters. This was somewhat expected, since the distribution of the duration of price spells inferred purely from aggregate data is already quite similar to the empirical distribution. As such, we take this estimation exercise as an illustration of the potential for incorporating a fraction of the vast amounts of microeconomic information about pricing behavior produced by the empirical literature into the estimation of macroeconomic models of price setting.

### 4.3 Comparison with homogeneous-firms models

In this subsection we ask how sharply the data allow us to discriminate between multi-sector models with heterogeneity in price stickiness and one-sector models with homogeneous firms. To that end we estimate one-sector models with price spells ranging from two to eight quarters. We keep the same prior distributions for all parameters besides the sectoral weights. A one-sector model with price spells of length k, say, can be seen as a restriction of the more general heterogeneous model, with a prior over the distribution of sectoral weights that puts probability one on  $\omega_k = 1$ .

We pick the best-fitting one-sector model according to the marginal density of the data given the models. The results are reported in Table 6 and Figure 3. The best-fitting model is the one in which all price spells last for 7 quarters. This seems unreasonable in light of the micro-

methods to estimate a model with Taylor staggered price setting and heterogeneous price contracts of up to 4 quarters, and find an incredible amount of real rigidity. When estimating a version of our model with K=4 we also find substantially stronger pricing complementarities ( $\zeta$  tightly distributed around 0.006).

<sup>&</sup>lt;sup>30</sup>In previous versions of the paper we reported results with different degrees of prior tightness. The results reported here are representative of what we learn from alternative configurations.

Table 5: Parameter estimates for the U.S. economy - informative prior

	Model	$l \ with \ K = 8, \ \alpha_0 =$	= 80	Empirical distribution
ζ	4.440 (0.47;16.86)	$0.049 \\ (0.022; 0.114)$	0.047	_
$\omega_1$	$0.256 \atop (0.18; 0.34)$	0.132 (0.103;0.166)	0.28	0.27
$\omega_2$	0.073 $(0.03;0.13)$	0.125 $(0.097; 0.157)$	0.07	0.07
$\omega_3$	0.097 $(0.05;0.16)$	0.112 $(0.087; 0.142)$	0.07	0.10
$\omega_4$	0.108 $(0.06;0.17)$	0.116 $(0.090; 0.147)$	0.09	0.11
$\omega_5$	0.063 $(0.03;0.12)$	0.128 $(0.099; 0.161)$	0.07	0.06
$\omega_6$	0.126 $(0.07;0.19)$	0.128 $(0.099; 0.161)$	0.14	0.13
$\omega_7$	0.064 $(0.03;0.12)$	0.126 $(0.098; 0.159)$	0.07	0.06
$\omega_8$	0.188 $(0.12;0.27)$	0.125 $(0.097; 0.158)$	0.20	0.20
$ar{k}$	4.258 (3.79;4.74)	4.508 (4.299;4.719)	4.28	4.25
$\sigma_k$	$2.610 \\ (2.42;2.78)$	$\begin{array}{c} 2.312 \\ (2.221; 2.403) \end{array}$	2.69	2.66
$ ho_0$	$0.000 \\ (-8.22; 8.22)$	$0.000 \\ (-0.001; 0.001)$	0.000	_
$\rho_1$	0.000 $(-8.22;8.22)$	1.431 $(1.278;1.582)$	1.428	_
$\rho_2$	0.000 $(-8.22;8.22)$	-0.451 $(-0.599; -0.301)$	-0.448	_
$\sigma_m$	$0.059 \atop (0.01; 0.20)$	0.005 $(0.005;0.006)$	0.005	_
$\delta_0$	$0.000 \\ (-8.22; 8.22)$	0.003 $(-0.003;0.009)$	0.002	_
$\delta_1$	0.000 $(-8.22;8.22)$	$0.395 \ (0.218; 0.579)$	0.543	_
$\delta_2$	0.000 $(-8.22;8.22)$	0.183 $(0.043;0.322)$	0.150	_
$\sigma_n$	0.059 $(0.01;0.20)$	0.102 $(0.044;0.223)$	0.077	_

Note: The first two columns report the medians for, respectively, the marginal prior and posterior distributions; the third column gives the mean of the marginal posterior distribution; numbers in parentheses correspond to the  $5^{\rm th}$  and  $95^{\rm th}$  percentiles; the last column reproduces the empirical distribution from Table 2.

economic evidence. Given the extent of nominal rigidity, not surprisingly the degree of pricing complementarity is smaller. The posterior distributions for the parameters of the nominal output process are quite similar to the ones obtained in the multi-sector models. Perhaps this should be expected given that this variable is one of the observables used in the estimation. In contrast, the distributions of the parameters of the unobserved driving process are quite different under the restriction of homogeneous firms. We defer a discussion of what might drive this result to the end of this subsection.

Table 6: Best-fitting model with homogeneous firms

	Prior	$K=7,\omega_7$	= 1
ζ	4.440	0.362	0.419
-	(0.466;16.863)	(0.193; 0.830)	
$ ho_0$	0.000	0.000	0.000
	(-8.224; 8.224)	(-0.001;0.001)	1 400
$ ho_1$	$0.000 \\ (-8.224; 8.224)$	$\frac{1.430}{(1.284;1.568)}$	1.428
	0.000	-0.454	-0.452
$ ho_2$	(-8.224; 8.224)	-0.454 (-0.590; -0.310)	-0.452
$\sigma_m$	0.059	0.005	0.005
$o_m$	(0.009;0.195)	(0.005;0.006)	0.000
$\delta_0$	0.000	0.003	0.004
00	(-8.224; 8.224)	(-0.003; 0.011)	0.001
$\delta_1$	0.000	0.064	0.071
	(-8.224; 8.224)	(-0.154; 0.319)	
$\delta_2$	0.000	0.135	0.141
_	(-8.224;8.224)	(-0.027; 0.327)	0.990
$\sigma_n$	0.059 $(0.009; 0.195)$	0.216 $(0.087;0.421)$	0.230
	(0.000,0.100)	(5.551,0.121)	

Note: The first two columns report the medians for, respectively, the marginal prior and posterior distributions; the third column gives the mean of the marginal posterior distribution; numbers in parentheses correspond to the  $5^{\rm th}$  and  $95^{\rm th}$  percentiles.

Table 7 reports the marginal density of the data given the three models analyzed so far: the multi-sector model with the flat prior for  $\omega$  ( $\alpha_0 = 8$ ), the multi-sector model with the informative prior ( $\alpha_0 = 80$ ), and the best-fitting one-sector model. It also reports the average duration of price spells ( $\bar{k}$ ) and the cross-sectional standard deviation of the sectoral distribution of price spells ( $\sigma_k$ ) computed with the means of the marginal distributions as point estimates for the sectoral weights. The fit of the two multi-sector models is very similar. In contrast, the performance of the best-fitting one-sector model is much worse. The posterior odds in favor of the heterogeneous models is of the order of  $10^{11}$ : 1.

To shed light on why the multi-sector models perform so much better than the homogeneous models we compare model-implied dynamics for inflation and output to those of a restricted bivariate VAR including nominal and real output. In estimating the VAR we impose the same assumption used in the model, that nominal output is exogenous and follows an AR(2) process.

Table 7: Model comparison

	$K = 8,  \alpha_0 = 8$	$K = 8,  \alpha_0 = 80$	$K=7,\omega_7=1$
$ar{k}$	4.37	4.28	7.0
$\sigma_k$	2.62	2.69	zero
log MPD	808.03	807.53	781.33

Note: The logarithm of the marginal posterior density of the data given the models (log MPD) is approximated with Geweke's (1999) modified harmonic mean.

We allow real output to depend on four lags of both itself and nominal output, and to be contemporaneously affected by innovations to nominal output. Estimation is by ordinary least squares. The multi-sector model is the one estimated under flat priors for  $\omega$ , while the one-sector model is the one with the best fit. The parameter values are fixed at their posterior means.

The panel in Figure 4 shows the impulse response functions of output  $(y_t)$ , left column) and inflation  $(\pi_t)$ , right column) to positive innovations  $\varepsilon_t^m$  (top row) and  $\varepsilon_t^n$  (bottom row) of one standard deviation in size. Relative to the one-sector model, the estimated multi-sector model does a better job at approximating the impulse response functions produced by the VAR at both short and medium horizons, in response to both shocks. Thus the overwhelming statistical support for heterogeneity does not seem to depend on any single feature of the dynamic response of macroeconomic variables to the shocks. Finally, these results suggest one explanation for why the estimated parameters associated with the unobserved driving process are so different in the one-sector economy. While the multi-sector model can rely on the distribution of sectoral weights to balance the response of the economy to shocks at different horizons, the one-sector model lacks this mechanism. Given the facts that nominal output is observed and that its parameter estimates imply quite persistent dynamics in both economies, perhaps the one-sector economy needs to rely on the unobserved process as a more transient and volatile component that can help it do a better job at matching higher-frequency features of the data.

### 5 Results for other countries

We provide estimates of the cross-sectional distribution of price stickiness implied by the aggregate data for ten additional countries: Australia, Canada, Denmark, France, Italy, Korea, Norway, Sweden, Switzerland, and the U.K.. Among these countries, we are aware of studies reporting price-setting statistics based on micro data for Canada (Harchaoui et al. 2008), Denmark (Hansen and Hansen 2006), France (Baudry et al. 2007), Italy (Fabiani et al. 2006), Norway (Wulfsberg 2009), Switzerland (Kaufmann 2008), and the U.K. (Bunn and Ellis 2009).

With the exception of Canada, we have access to the cross-sectional price-setting statistics for those countries.<sup>31</sup> Unfortunately, Denmark is the only case where the level of detail in the cross-section is comparable to the studies for the U.S. economy: it includes statistics for 391 goods and services categories at the COICOP 5-digit level. The papers for Switzerland, France and Italy also provide statistics at the same level of disaggregation, but for 139, 136 and 48 categories, respectively. Wulfsberg (2009) provides statistics for Norway for 89 4-digit COICOP classes. Finally, Bunn and Ellis (2009) provide much more aggregated statistics for the U.K. (which are not useful for our purposes).

Due to the limited cross-sectional information available in most studies, we focus on a comparison between the average duration of price spells  $(\bar{k})$  and cross-sectional standard deviation of the sectoral distribution of price spells  $(\sigma_k)$  implied by our macro-based estimates, and their empirical counterparts. The latter are constructed according to the methodology described in Subsection 3.1. The results are summarized in Table 8. Countries are ranked (roughly) in descending order in terms of available level of detail about the cross-section of interest. Perhaps with the exception of the cross-sectional standard deviation of the duration of price spells in France, the results are broadly in line with the available microeconomic evidence. Our macro-based estimates even pick up the fact that France exhibits noticeably less price stickiness than the average in the Euro area (Dhyne et al. 2006).

Given the level of detail available for Denmark, we provide a more detailed comparison between our macro-based estimates and the empirical distribution. The results are presented in Table 9. Using the posterior means as the point estimates for the sectoral weights - reported in the third column of numbers - 30% of firms change prices every quarter; 54% change prices at least once a year; 17% change prices once every two years. The average duration of price spells is 13.7 months, and the standard deviation of the (cross-sectional) distribution of price spells is approximately 8.3 months. With the exception of the split of weights between the first two sectors, the estimated distribution is quite close to the empirical distribution. If we construct a 7-sector distribution by combining sectors one and two, the correlation with the empirical distribution is 0.85. The same correlation for the 8-sector estimated distribution is 0.31. For completeness, in the Appendix we report the full set of parameter estimates for the remaining countries.

# 6 Robustness and directions for future research

Our findings are robust to different prior assumptions for the parameters  $\rho_i$ ,  $\delta_i$ ,  $\sigma_m$ ,  $\sigma_n$  and  $\zeta$ , as well as different de-trending procedures and specifications for the exogenous time-series processes.

<sup>&</sup>lt;sup>31</sup>We thank Niels Lynggård Hansen, Herve Le Bihan, Silvia Fabiani, Fredrik Wulfsberg, Daniel Kaufmann and Philip Bunn for providing us with the statistics from their respective papers.

Table 8: Estimates of moments of the cross-sectional distribution of price stickiness

	Model		-	pirical
	$K = 8,  \alpha_0 = 8$		$_{\_}$ distribution	
	$\frac{\overline{k}}{}$	$\sigma_k$	$\phantom{aaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaa$	$\sigma_k$
Denmark	4.58 $(3.21;5.73)$	$\frac{2.78}{(2.20;3.04)}$	4.77	2.60
$Switzerland^{1)}$	4.91 $(3.71;5.98)$	$\frac{2.39}{(1.81; 2.68)}$	4.87	2.52
France	$\frac{3.86}{(2.72;5.03)}$	$\frac{2.86}{(2.35;3.09)}$	3.20	1.60
$Italy^{2)}$	4.47 $(3.20;5.63)$	$\frac{2.67}{(2.07;2.93)}$	4.70	2.35
$Norway^{3)}$	$4.30 \\ (3.20;5.41)$	$\underset{(1.72;2.71)}{2.35}$	4.50	2.33
U.K.	4.46 $(3.22;5.71)$	$\frac{2.65}{(1.98;3.02)}$	_	_
Canada	4.65 $(3.34;5.88)$	$\frac{2.78}{(2.19;3.05)}$	_	_
Australia	4.98 $(3.65;6.16)$	$\frac{2.68}{(2.10;2.93)}$	_	_
Korea	4.52 $(3.24;5.74)$	$ \begin{array}{c} 2.72 \\ (2.14; 2.99) \end{array} $	_	_
Sweden	4.49 $(3.23;5.73)$	$\frac{2.67}{(1.99;3.02)}$	_	_

Note: Model-based estimates for the moments  $\bar{k}$  and  $\sigma_k$  are computed using the means of the marginal posterior distributions as the point estimates; umbers in parentheses correspond to the 5<sup>th</sup> and 95<sup>th</sup> percentiles; 1) Statistics based on the durations reported in Kaufmann (2008, Table 7); 2) Statistics based on the implied median durations reported in Fabiani et al. (2006, Table A3.1); 3) Durations for individual classes are scaled up proportionately so that the cross-sectional (weighted) average duration computed from the monthly statistics matches the mean duration reported by Wulfsberg (2009, Table 1) for the sub-period 1990-2004. This adjustment makes his statistics more comparable to those of the other countries, which are based on more recent samples covering periods of lower inflation.

In all cases that we analyzed we found overwhelming support for the models with heterogeneity.

We also considered versions of the models with Calvo (1983) pricing. In that case, not all of our conclusions are equally robust. The reason is that, in the context of our semi-structural framework, identification of heterogeneity in price stickiness under Calvo pricing is "more difficult" than under Taylor pricing. Building on Monte Carlo analysis and analytical insights from simple versions of these two pricing models, we found that clear-cut identification of the distribution of price stickiness depends crucially on whether the observable driving process has high variance relative to the unobservable process. While this applies to both price-setting specifications, the identification problem is more acute under Calvo pricing. The reason is that, in terms of implications for the aggregate dynamics of output and prices, the differences between specifications with varying degrees of price stickiness are much starker under Taylor pricing than under

Table 9: Parameter estimates for the Danish economy - flat prior

	Model v	with $K = 8$ , $\alpha_0 =$	: 8	$\frac{Empirical}{distribution}$
ζ	4.440 (0.466;16.863)	0.190 $(0.060; 0.586)$	0.240	
$\omega_1$	0.094 $(0.007; 0.348)$	0.283 $(0.109; 0.521)$	0.30	0.14
$\omega_2$	0.094 $(0.007; 0.348)$	0.051 $(0.004;0.170)$	0.06	0.18
$\omega_3$	0.094 $(0.007; 0.348)$	0.034 $(0.003; 0.125)$	0.05	0.04
$\omega_4$	0.094 $(0.007; 0.348)$	0.034 $(0.003; 0.133)$	0.05	0.09
$\omega_5$	0.094 $(0.007; 0.348)$	0.065 $(0.005; 0.239)$	0.09	0.12
$\omega_6$	0.094 $(0.007; 0.348)$	0.074 $(0.006; 0.264)$	0.10	0.07
$\omega_7$	0.094 $(0.007; 0.348)$	0.176 $(0.017; 0.458)$	0.20	0.11
$\omega_8$	0.094 $(0.007; 0.348)$	$0.147 \\ (0.014; 0.402)$	0.17	0.25
$ar{k}$	4.501 $(3.245;5.760)$	4.507 $(3.214;5.731)$	4.58	4.77
$\sigma_k$	$2.139 \\ (1.584; 2.678)$	$\begin{array}{c} 2.668 \\ (2.203; 3.044) \end{array}$	2.78	2.60
$ ho_0$	$0.000 \ (-8.224; 8.224)$	$ \begin{array}{c} 0.001 \\ (-0.001; 0.003) \end{array} $	0.001	_
$ ho_1$	$0.000 \\ (-8.224; 8.224)$	0.774 $(0.607; 0.938)$	0.774	_
$ ho_2$	$0.000 \\ (-8.224; 8.224)$	0.183 $(0.020; 0.348)$	0.183	_
$\sigma_m$	0.059 $(0.009;0.195)$	0.013 $(0.011;0.014)$	0.013	_
$\delta_0$	0.000 $(-8.224;8.224)$	0.001 $(-0.004;0.007)$	0.001	_
${\delta}_1$	0.000 $(-8.224;8.224)$	0.297 $(0.063; 0.505)$	0.292	_
$\delta_2$	0.000 $(-8.224;8.224)$	0.299 $(0.147;0.449)$	0.298	_
$\sigma_n$	0.059 $(0.009; 0.195)$	$0.065 \ (0.032; 0.171)$	0.079	_

Note: The first two columns report the medians for, respectively, the marginal prior and posterior distributions; the third column gives the mean of the marginal posterior distribution; numbers in parentheses correspond to the 5<sup>th</sup> and 95<sup>th</sup> percentiles; the last column reproduces the empirical distribution obtained by applying the steps described in Subsection 3.1 to the statistics reported in Hansen and Hansen (2006).

Calvo pricing. Based on Monte Carlo analysis, we found that with the sample size that we have and the relative variances for the two exogenous processes implied by our point estimates, the likelihood criterion fails to provide a sharp discrimination between alternative (non-degenerate) distributions of price stickiness under Calvo pricing. This mirrors what we find in the data: under Calvo pricing they do not allow clear discrimination between models with heterogeneity in the frequency of price changes. In contrast, given the same sample size and relative variances for those two processes, the version of the model with Taylor pricing provides more information about the underlying distribution of price stickiness.

However, despite that obstacle, the main finding of the paper does hold under the Calvo pricing model: the (log) posterior density of the data given specifications with heterogeneity in price stickiness is roughly 5-7 points higher than under the best specification with homogeneous firms. In addition, using classical methods we find that a likelihood-ratio test of the homogeneous Calvo model against a two-sector version of the model leads to rejection of the former at significance levels of less than 1%.

More generally, our experience based on specifications with Taylor and Calvo pricing models suggests that the shape of the hazard function for price adjustments assumed in the price-setting model is important in determining how precisely the cross-sectional distribution of price stickiness can be inferred from aggregate data. An interesting way to address this question would be to specify a generalized pricing model with a more flexible price adjustment hazard than in the Calvo and Taylor models, and take the model to the data allowing for sectoral heterogeneity in the hazards.<sup>33</sup> The question, then, would be how to use the microeconomic evidence on price setting to inform the priors over the nature of such adjustment hazard functions. One alternative would be to use a parsimonious parametric family of hazard functions, say a two-parameter family characterized by level and slope of the hazard. Then, one could use the microeconomic evidence on the frequency of price changes and on the shape of adjustment hazard functions estimated from microeconomic data (e.g. Klenow and Kryvtsov 2008) to form priors over those two parameters, and estimate the model using aggregate data as observables, as we do.

Allowing for more general adjustment hazards also holds the promise of reconciling the macroeconomic model with other microeconomic features of price setting documented in the recent empirical literature, from which we abstract completely. For example, Klenow and Kryvtsov

 $<sup>^{32}</sup>$ The likelihood-ratio statistic ranges from roughly 10.5 to 14 (depending on the specification for the exogenous time-series processes), whereas the 0.1% and 1% critical values for the  $\chi^2$  (1) distribution are, respectively, 10.83 and 6.64.

<sup>&</sup>lt;sup>33</sup>Dotsey et al. (1997) proposed such a generalized price-setting model, assuming that all firms are ex-ante identical. Similar specifications have been used subsequently by Wolman (1999) and Mash (2004), among others. Coenen et al. (2007), Guerrieri (2006), Sheedy (2007), and Yao (2009) estimate models with generalized price-setting hazards using aggregate data. To our knowledge the only paper to allow for generalized adjustment hazards and ex-ante heterogeneity in models of price setting is Carvalho and Schwartzman (2008).

(2008) document time-variation in the duration of price spells. While this is at odds with our assumption of Taylor price contracts, it is consistent with models of price setting with different adjustment-hazard functions.

Finally, we wish to emphasize that our results do not imply that identification of more nuanced features of the distribution of price stickiness from aggregate data is infeasible under Calvo pricing. In fact, as we show in the Appendix, in this version of the model the sectoral weights are also identified in the formal sense. However, our findings do suggest that, in practice, additional structure is needed for estimation. It is possible that additional restrictions obtained by moving to a fully-specified model and using additional observables in the estimation will impose more "discipline" on the latent stochastic processes and thus attenuate the problems we encountered with Calvo pricing in our semi-structural framework. In addition, making use of sectoral data as well, along the lines of Lee (2009) and Bouakez et al. (2009), seems promising.

## 7 Conclusion

We estimate small semi-structural models for the U.S. economy in which the extent of price rigidity varies across firms. We provide estimates of the underlying cross-sectional distribution based only on aggregate data, and estimates that incorporate prior microeconomic information from the recent empirical price-setting literature. Perhaps surprisingly, we find that the former accords quite well with the latter evidence. More generally, we find overwhelming evidence in favor of specifications with heterogeneity in price stickiness, over ones in which all prices are equally sticky.

We find the results sufficiently compelling to warrant further research. In particular, it would be interesting to evaluate the consequences of allowing for heterogenous pricing behavior when estimating fully-specified models DSGE. The experience with our semi-structural model suggests that combining microeconomic information and macroeconomic data within a Bayesian framework can help us integrate our views on price setting at the microeconomic and macroeconomic levels. Quantitative normative analysis in models with heterogeneity in price stickiness, along the lines of Eusepi et al. (2009), might also benefit from such a combination.

# Appendix

# A Identification when $\zeta \neq 1$

When  $\zeta \neq 1$  equation (12) becomes

$$p_t = \sum_{j=1}^{K-1} a_j p_{t-j} + \sum_{j=0}^{K-1} b_j m_{t-j} - \sum_{j=0}^{K-1} b_j y_{t-j}^n,$$

where  $a_1,..., a_{K-1}, b_0, ..., b_{K-1}$  are complicated functions of the model parameters. Checking for identification amounts to solving for these coefficients to show that  $\omega_1,...,\omega_K$  and  $\zeta$  can be recovered from them.

In practice the mathematical expressions involved are extremely long, and the exercise is all but infeasible, except for models with a small number of sectors. Here we illustrate how the process works in a model with K = 2. Using the method of undetermined coefficients we can show that  $a_1, b_0, b_1$  satisfy:

$$a_{1} = \frac{\frac{\omega_{2}}{2} \frac{1-\beta}{1-\beta^{2}} (1-\zeta)}{1-\left(\left(\omega_{1} + \frac{\omega_{2}}{2} \frac{1-\beta}{1-\beta^{2}} (1+\beta)\right) (1-\zeta) + \left(\frac{\omega_{2}}{2} \frac{1-\beta}{1-\beta^{2}} \beta\right) (1-\zeta)a_{1}\right)}$$

$$b_{0} = \frac{\left(\omega_{1} + \frac{\omega_{2}}{2} \frac{1-\beta}{1-\beta^{2}} (1+\beta)\right) \zeta + \left(\frac{\omega_{2}}{2} \frac{1-\beta}{1-\beta^{2}} \beta\right) (\zeta \rho + (1-\zeta)b_{1})}{1-\left(\left(\omega_{1} + \frac{\omega_{2}}{2} \frac{1-\beta}{1-\beta^{2}} (1+\beta)\right) (1-\zeta) + \left(\frac{\omega_{2}}{2} \frac{1-\beta}{1-\beta^{2}} \beta\right) (1-\zeta)a_{1}\right) - \left(\frac{\omega_{2}}{2} \frac{1-\beta}{1-\beta^{2}} \beta\right) (1-\zeta)\rho}$$

$$b_{1} = \frac{\frac{\omega_{2}}{2} \frac{1-\beta}{1-\beta^{2}} \zeta}{1-\left(\left(\omega_{1} + \frac{\omega_{2}}{2} \frac{1-\beta}{1-\beta^{2}} (1+\beta)\right) (1-\zeta) + \left(\frac{\omega_{2}}{2} \frac{1-\beta}{1-\beta^{2}} \beta\right) (1-\zeta)a_{1}\right)}.$$

The first equation is quadratic in  $a_1$  and for each solution the other two equations yield  $b_0$  and  $b_1$  as a function of the model parameters. The stable solution for the first equation ( $|a_1| \le 1$ ) yields:

$$a_{1} = \frac{(1+\beta)(2\zeta+(1-\zeta)\omega_{2})+\sqrt{(1+\beta)^{2}((\zeta-1)\omega_{2}-2\zeta)^{2}-4\beta(\zeta-1)^{2}\omega_{2}^{2}}}{2\beta(1-\zeta)\omega_{2}}$$

$$b_{0} = \frac{\zeta(\rho-1)(\rho\beta-1)\omega_{2}}{2(1+\beta)\rho\zeta+(\zeta-1)(\rho-1)(\rho\beta-1)\omega_{2}} + \frac{\zeta(1+\beta)(1+\beta(1+2\rho(\zeta-1)))}{\beta(\zeta-1)(2(1+\beta)\rho\zeta+(\zeta-1)(\rho-1)(\rho\beta-1)\omega_{2})}$$

$$-\zeta(1+\beta)\frac{(1+\beta)2\zeta+\sqrt{4(1+\beta)^{2}\zeta^{2}-4(1+\beta)^{2}(\zeta-1)\zeta\omega_{2}+(\beta-1)^{2}(\zeta-1)^{2}\omega_{2}^{2}}}{\beta(\zeta-1)^{2}\omega_{2}(2(1+\beta)\rho\zeta+(\zeta-1)(\rho-1)(\rho\beta-1)\omega_{2})}$$

$$b_{1} = \zeta\frac{(1+\beta)(2\zeta+(1-\zeta)\omega_{2})+\sqrt{(1+\beta)^{2}((\zeta-1)\omega_{2}-2\zeta)^{2}-4\beta(\zeta-1)^{2}\omega_{2}^{2}}}{2\beta(1-\zeta)^{2}\omega_{2}},$$

where we have used the fact that  $\omega_1 + \omega_2 = 1$ . Finally we can the combine the expressions for  $a_1$ 

and  $b_1$  to solve for  $\omega_2$  and  $\zeta$ :

$$\omega_2 = \frac{2(1+\beta)b_1}{(1-a_1)(1-\beta a_1)}$$

$$\zeta = \frac{b_1}{a_1+b_1}.$$

# B Identification in a multi-sector Calvo (1983) model

Under the assumption of Calvo pricing, equations (6) and (5) are replaced by, respectively:

$$x_t(k) = (1 - \beta \alpha_k) E_t \sum_{i=0}^{\infty} (\alpha_k \beta)^i \left( p_{t+i} + \zeta \left( y_{t+i} - y_{t+i}^n \right) \right), \tag{13}$$

and

$$p_t(k) = \int_0^1 p_t(k, j) dj = (1 - \beta \alpha_k) \sum_{i=0}^{\infty} \alpha_k^{-i} x_{t-i}(k),$$

where  $1 - \alpha_k$  is the frequency of price changes in sector k. The remaining equations of the model are:

$$p_{t} = \sum_{k=1}^{K} \omega_{k} p_{t} (k)$$

$$p_{t} + y_{t} = m_{t} = \rho_{1} m_{t-1} + \sigma_{m} \widetilde{\varepsilon}_{t}^{m}$$

$$y_{t}^{n} = \delta_{1} y_{t-1}^{n} + \sigma_{n} \widetilde{\varepsilon}_{t}^{n}.$$

We focus on the case of strategic neutrality in price setting ( $\zeta = 1$ ). Then, (13) simplifies to:

$$x_{t}(k) = (1 - \beta \alpha_{k}) E_{t} \sum_{i=0}^{\infty} (\alpha_{k} \beta)^{i} (m_{t+i} - y_{t+i}^{n})$$
$$= F(\beta, \rho_{1}, \alpha_{k}) m_{t} - F(\beta, \delta_{1}, \alpha_{k}) y_{t}^{n}.$$

In that case the aggregate price level evolves according to:

$$p_{t} = \sum_{j=0}^{\infty} \sum_{k=1}^{K} \omega_{k} (1 - \beta \alpha_{k}) F(\beta, \rho_{1}, \alpha_{k}) \alpha_{k}^{-j} m_{t-j}$$
$$- \sum_{j=0}^{\infty} \sum_{k=1}^{K} \omega_{k} (1 - \beta \alpha_{k}) F(\beta, \delta_{1}, \alpha_{k}) \alpha_{k}^{-j} y_{t-j}^{n}.$$

We illustrate how identification obtains in a model with K=2. As in Subsection 2.4, the starting point is a set of consistent estimates of the coefficients on  $m_{t-j}$  ( $\sum_{k=1}^{K} \omega_k (1 - \beta \alpha_k) F(\beta, \rho_1, \alpha_k) \alpha_k^{-j}$ ),

which we denote by  $a_i$ . With K=2, this implies the following system of equations:

$$\omega_{1} (1 - \beta \alpha_{1}) F (\beta, \rho_{1}, \alpha_{1}) + (1 - \omega_{1}) (1 - \beta \alpha_{2}) F (\beta, \rho_{1}, \alpha_{2}) = a_{0}$$

$$\omega_{1} (1 - \beta \alpha_{1}) F (\beta, \rho_{1}, \alpha_{1}) \alpha_{1}^{-1} + (1 - \omega_{1}) (1 - \beta \alpha_{2}) F (\beta, \rho_{1}, \alpha_{2}) \alpha_{2}^{-1} = a_{1}$$

$$\omega_{1} (1 - \beta \alpha_{1}) F (\beta, \rho_{1}, \alpha_{1}) \alpha_{1}^{-2} + (1 - \omega_{1}) (1 - \beta \alpha_{2}) F (\beta, \rho_{1}, \alpha_{2}) \alpha_{2}^{-2} = a_{2},$$

which can be solved for  $\omega_1$ ,  $\alpha_1$ , and  $\alpha_2$  as a function of  $a_0$ ,  $a_1$  and  $a_2$  (and  $\beta$ ,  $\rho_1$ ).

# C Details of the estimation algorithm

Our specific estimation strategy is as follows. We run two numerical optimization routines sequentially in order to maximize the posterior distribution. This determines the starting point of the Markov chain and provides a first crude estimate of the covariance matrix for our Random-Walk Metropolis Gaussian jumping distribution. The first optimization routine is csminwel by Chris Sims, while the second is fminsearch from Matlab's optimization toolbox. For the starting values, we set  $\zeta = 1$  and  $\omega_k = 1/K$ ; the values for the remaining parameters are set equal to the ordinary least squares estimates based on nominal output (for the  $\rho$ 's) and actual output (for the  $\delta$ 's). Following the first optimization, we run additional rounds, starting from initial values obtained by perturbing the original initial values, and then the estimate of the first optimization round.

Before running the Markov chains we transform all parameters to have full support on the real line. We use the logarithmic transformation for each of  $(\zeta, \sigma_m, \sigma_n)$ , while  $\omega_1, ..., \omega_K$  are transformed using a multivariate logistic function (see next subsection). Then we run a so-called adaptive phase of the Markov chain, with three sub-phases of 100, 200, and 600 thousand iterations, respectively. At the end of each sub-phase we discard the first half of the draws, update the estimate of the posterior mode, and compute a sample covariance matrix to be used in the jumping distribution in the next sub-phase. Finally, in each sub-phase we rescale the covariance matrix inherited from the previous sub-phase in order to get a fine-tuned covariance matrix that yields rejection rates as close as possible to 0.77.<sup>34</sup> Next we run the so-called fixed phase of the MCMC. We take the estimate of the posterior mode and sample covariance matrix from the adaptive phase, and run 5 parallel chains of 300,000 iterations each. Again, before making the draws that will form the sample we rescale such covariance matrix in order to get rejection rates as close as possible to 0.77. To initialize each chain we draw from a candidate normal distribution centered on the posterior mode estimate, with covariance matrix given by 9 times the fine-tuned covariance matrix. We check for convergence for the latter 2/3s of the draws of all 5 chains by

<sup>&</sup>lt;sup>34</sup>This is the optimal rejection rate under certain conditions. See Gelman et al. (2003, p. 306).

calculating the potential scale reduction<sup>35</sup> (PSR) factors for each parameter and inspecting the histograms of all marginal distributions across the parallel chains. Upon convergence, the latter 2/3s of the draws of all 5 chains are combined to form a posterior sample of 1 million draws.

### C.1 Transformation of the sectoral weights

We transform vectors  $\omega = (\omega_1, ..., \omega_K)$  in the K-dimensional unit simplex into vectors  $v = (v_1, ..., v_K)$  in  $\mathbb{R}^K$  using the inverse of a restricted multivariate logistic transformation. We want to be able to draw v's and then use a transformation that guarantees that  $\omega = h^{-1}(v)$  is in the K-dimensional unit simplex. For that purpose, we start with:

$$\omega_k = \frac{e^{v_k}}{\sum_{k=1}^K e^{v_k}}, k = 1, ..., K.$$

The transformation above guarantees the non-negativity and summation to unity constraints. However, without additional restrictions the mapping is not one-to-one. The reason is that all vectors v along the same ray give rise to the same  $\omega$ . Therefore, we impose the restriction v(K) = 0 and in effect draw vectors  $\tilde{v} = (v_1, ..., v_{K-1})$  in  $\mathbb{R}^{K-1}$ . Thus, the transformation becomes  $\tilde{\omega} = \tilde{h}^{-1}(\tilde{v})$ , with  $\tilde{\omega} = (\omega_1, ..., \omega_{K-1})$  and:

$$\omega_k = \frac{e^{v_k}}{1 + \sum_{k=1}^{K-1} e^{v_k}}, k = 1, ..., K - 1$$

$$\omega_K = \frac{1}{1 + \sum_{k=1}^{K-1} e^{v_k}}.$$

If the density  $f_{\omega}(\omega|\alpha)$  is that of the Dirichlet distribution with (vector) parameter  $\alpha$ , the density of  $\widetilde{v}$  is given by:

$$f_{\widetilde{v}}(\widetilde{v}|\alpha) = |J|f_{\omega}\left(\frac{e^{v_1}}{1 + \sum_{k=1}^{K-1} e^{v_k}}, ..., \frac{1}{1 + \sum_{k=1}^{K-1} e^{v_k}}|\alpha\right),$$

<sup>&</sup>lt;sup>35</sup>For each parameter, the PSR factor is the ratio of (square root of) an estimate of the marginal posterior variance to the average variance within each chain. This factor expresses the potential reduction in the scaling of the estimated marginal posterior variance relative to the true distribution by increasing the number of iterations in the Markov-chain algorithm. Hence, as the PSR factor approaches unity, it is a sign of convergence of the Markov-chain for the estimated parameter. See Gelman et al. (2003, p. 294 ff) for more information. For all specifications we require that the factor be below 1.01 for all parameters.

where |J| is the determinant of the Jacobian matrix  $\left[\frac{\partial \tilde{h}^{-1}(\tilde{v})}{\partial \tilde{v}}\right]_{ij}$  given by:

$$\begin{bmatrix} \frac{\partial \omega_1}{\partial v_1} & \frac{\partial \omega_1}{\partial v_2} & \cdots & \frac{\partial \omega_1}{\partial v_{K-1}} \\ \frac{\partial \omega_2}{\partial v_1} & \frac{\partial \omega_2}{\partial v_2} & \cdots & \frac{\partial \omega_2}{\partial v_{K-1}} \\ \vdots & \vdots & \ddots & \vdots \\ \frac{\partial \omega_{K-1}}{\partial v_1} & \frac{\partial \omega_{K-1}}{\partial v_2} & \cdots & \frac{\partial \omega_{K-1}}{\partial v_{K-1}} \end{bmatrix},$$

with:

$$\frac{\partial \omega_k}{\partial v_k} = \frac{e^{v_k} \left( 1 + \sum_{k=1}^{K-1} e^{v_k} \right) - e^{v_k} e^{v_k}}{\left( 1 + \sum_{k=1}^{K-1} e^{v_k} \right)^2} \\
= \frac{e^{v_k}}{1 + \sum_{k=1}^{K-1} e^{v_k}} - \frac{e^{v_k} e^{v_k}}{\left( 1 + \sum_{k=1}^{K-1} e^{v_k} \right)^2}.$$

So:

$$J = -\left[\begin{array}{c} \frac{e^{v_1}}{1 + \sum_{k=1}^{K-1} e^{v_k}} \\ \vdots \\ \frac{e^{v_{K-1}}}{1 + \sum_{k=1}^{K-1} e^{v_k}} \end{array}\right] \left[\frac{e^{v_1}}{1 + \sum_{k=1}^{K-1} e^{v_k}}, \dots, \frac{e^{v_{K-1}}}{1 + \sum_{k=1}^{K-1} e^{v_k}}\right] + \left[\begin{array}{cccc} \frac{e^{v_1}}{1 + \sum_{k=1}^{K-1} e^{v_k}} & 0 & \dots & 0 \\ 0 & \ddots & 0 & \vdots \\ \vdots & 0 & \ddots & 0 \\ 0 & \dots & 0 & \frac{e^{v_{K-1}}}{1 + \sum_{K-1}^{K-1} e^{v_k}} \end{array}\right].$$

To recover the  $v_k$ 's from  $\omega$  simply set:

$$v_k = \log(\omega_k) - \log(\omega_K).$$

# D Estimates for other countries

Tables 10 and 11 present the full set of estimates for the remaining countries:

Table 10: Parameter estimates for remaining countries - K=8, flat prior

	D :	0 1 1 1		T, 1	3.7
	Prior	Switzerland	France	Italy	Norway
ζ	4.440	0.403	0.193	1.272	8.068
	(0.466;16.863)	(0.103; 1.387)	(0.074; 0.474)	(0.479; 3.312)	(3.157;18.516)
$\omega_1$	0.094	0.072	0.365	0.278	0.128
	(0.007; 0.348)	(0.016; 0.233)	(0.143; 0.615)	(0.105; 0.519)	(0.028; 0.335)
$\omega_2$	0.094	0.043	0.058	0.027	0.163
	(0.007;0.348)	(0.003;0.190)	(0.005;0.205)	(0.002;0.106)	(0.022;0.383)
$\omega_3$	0.094	0.219	0.110	0.055	0.055
	(0.007; 0.348) 0.094	(0.088; 0.359) 0.080	(0.016; 0.234) 0.045	$(0.005; 0.169) \\ 0.037$	(0.004; 0.206) 0.089
$\omega_4$	(0.007;0.348)	(0.007;0.236)	(0.003; 0.170)	(0.003; 0.137)	(0.008;0.309)
(.1-	0.094	0.109	0.029	0.077	0.123
$\omega_5$	(0.007; 0.348)	(0.010;0.305)	(0.002;0.119)	(0.006; 0.255)	(0.010;0.398)
$\omega_6$	0.094	0.050	0.034	0.070	0.070
0	(0.007; 0.348)	(0.004; 0.191)	(0.002; 0.134)	(0.006; 0.237)	(0.006; 0.264)
$\omega_7$	0.094	0.061	0.049	0.271	0.098
•	(0.007; 0.348)	(0.005; 0.203)	(0.004; 0.187)	(0.051; 0.523)	(0.008; 0.341)
$\omega_8$	0.094	0.255	0.221	0.067	0.087
	(0.007; 0.348)	(0.061; 0.467)	(0.083; 0.385)	(0.003; 0.276)	(0.007; 0.313)
_					
$ar{k}$	4.501	4.940	3.848	4.496	4.305
	(3.245;5.760)	(3.711; 5.979)	(2.718; 5.028)	(3.203;5.633)	(3.198; 5.410)
$\sigma_k$	2.139	2.284	2.785	2.562	2.235
	(1.584; 2.678)	(1.812; 2.683)	(2.350;3.088)	(2.067; 2.925)	(1.720; 2.713)
	0.000	0.000	0.000	0.000	0.000
$ ho_0$	$0.000 \\ (-8.224; 8.224)$	$0.000 \\ (-0.001; 0.002)$	-0.000	-0.000	0.002
	, , ,		(-0.001;0.001)	(-0.002;0.001)	(-0.002;0.006)
$ ho_1$	$0.000 \\ (-8.224; 8.224)$	$\frac{1.528}{(1.382;1.671)}$	$ \begin{array}{c} 1.610 \\ (1.492;1.726) \end{array} $	$\frac{1.523}{(1.387; 1.657)}$	0.920 $(0.748;1.091)$
	0.000	-0.547	-0.618	-0.534	-0.011
$ ho_2$	(-8.224; 8.224)	(-0.690; -0.403)	-0.018 $(-0.734; -0.500)$	-0.554 (-0.670; -0.398)	(-0.184; 0.162)
$\sigma$	0.059	0.006	0.005	0.009	0.022
$\sigma_m$	(0.009; 0.195)	(0.006; 0.007)	(0.004; 0.006)	(0.008;0.010)	(0.020; 0.025)
		, , ,	, , ,	, ,	
$\delta_0$	0.000	0.001	0.000	0.000	-0.000
00	(-8.224; 8.224)	(-0.002; 0.006)	(-0.002; 0.002)	(-0.001;0.002)	(-0.003; 0.003)
$\delta_1$	0.000	0.223	0.770	0.862	0.461
~ 1	(-8.224; 8.224)	(-0.081; 0.771)	(0.442; 1.037)	(0.589; 1.110)	(0.248; 0.642)
$\delta_2$	0.000	0.454	0.137	0.062	0.441
-	(-8.224; 8.224)	(0.093; 0.676)	(-0.111; 0.419)	(-0.169; 0.311)	(0.261; 0.639)
$\sigma_n$	0.059	0.030	0.012	0.009	0.016
	(0.009;0.195)	(0.012;0.107)	(0.008;0.025)	(0.007;0.013)	(0.014;0.020)

Note: The first column reports the medians for the marginal prior distributions; the other columns provide the analogous statistics for the posterior marginal distributions in each country; numbers in parentheses correspond to the  $5^{\rm th}$  and  $95^{\rm th}$  percentiles.

Table 11: Parameter estimates for remaining countries - K=8, flat prior, continued

	Prior	U.K.	Canada	Australia	Korea	Sweden
ζ	$4.440 \\ (0.466; 16.863)$	$\underset{(1.269;10.330)}{3.681}$	$ \begin{array}{c} 1.040 \\ (0.389; 2.776) \end{array} $	0.599 $(0.231;1.490)$	0.556 $(0.102;1.630)$	$3.035 \\ (1.053; 8.697)$
$\omega_1$	$\underset{(0.007;0.348)}{0.094}$	$0.254 \atop (0.100; 0.484)$	0.253 $(0.090; 0.490)$	0.197 $(0.069; 0.417)$	$\underset{(0.064;0.452)}{0.211}$	0.247 $(0.086; 0.488)$
$\omega_2$	0.094 $(0.007; 0.348)$	$0.040 \\ (0.003; 0.153)$	$0.055 \\ (0.004; 0.181)$	$0.055 \\ (0.004; 0.178)$	$0.119 \atop (0.017; 0.271)$	$0.035 \ (0.003; 0.136)$
$\omega_3$	0.094 $(0.007; 0.348)$	0.037 $(0.003; 0.147)$	0.028 $(0.002;0.108)$	0.037 $(0.003; 0.130)$	0.037 $(0.003; 0.128)$	0.063 $(0.005; 0.222)$
$\omega_4$	0.094 $(0.007; 0.348)$	0.086 $(0.006; 0.304)$	$0.070 \ (0.006; 0.223)$	$0.035 \atop (0.003; 0.129)$	0.062 $(0.005; 0.197)$	0.078 $(0.006; 0.299)$
$\omega_5$	$0.094 \\ (0.007; 0.348)$	$0.072 \atop (0.005; 0.264)$	$0.054 \\ (0.004; 0.193)$	$0.065 \atop (0.006; 0.209)$	$0.078 \atop (0.007; 0.243)$	$0.046 \atop (0.003; 0.192)$
$\omega_6$	$0.094 \\ (0.007; 0.348)$	$0.093 \atop (0.007; 0.321)$	$0.060 \\ (0.005; 0.220)$	$0.114 \atop (0.012; 0.295)$	$0.078 \ (0.007; 0.248)$	$0.072 \\ (0.006; 0.272)$
$\omega_7$	$0.094 \\ (0.007; 0.348)$	$0.093 \atop (0.007; 0.315)$	0.147 $(0.015; 0.398)$	0.179 $(0.019; 0.430)$	$0.079 \atop (0.006; 0.271)$	$0.143 \atop (0.012; 0.413)$
$\omega_8$	$0.094 \\ (0.007; 0.348)$	$\underset{(0.014;0.444)}{0.158}$	$0.209 \atop (0.031; 0.461)$	$\underset{(0.030;0.443)}{0.210}$	$\underset{(0.037;0.451)}{0.219}$	$\substack{0.146 \\ (0.012; 0.425)}$
$ar{k}$	$4.501 \atop (3.245; 5.760)$	$4.456 \atop (3.220; 5.710)$	4.665 $(3.338;5.883)$	5.012 $(3.650;6.162)$	$4.529 \atop (3.241; 5.741)$	$\substack{4.501 \\ (3.231; 5.732)}$
$\sigma_k$	$\underset{(1.584; 2.678)}{2.139}$	$\substack{2.540 \\ (1.975; 3.020)}$	$\substack{2.685 \\ (2.195; 3.049)}$	$\underset{(2.102; 2.927)}{2.573}$	$\substack{2.615 \\ (2.137; 2.991)}$	$\substack{2.558 \\ (1.994; 3.022)}$
$ ho_0$	$0.000 \ (-8.224; 8.224)$	$-0.000 \ (-0.002;0.001)$	$\underset{(-0.001;0.002)}{0.001}$	$\underset{(-0.001;0.002)}{0.000}$	-0.001 $(-0.004;0.002)$	$\underset{(-0.001;0.003)}{0.001}$
$ ho_1$	$0.000 \ (-8.224; 8.224)$	$\underset{(1.034;1.363)}{1.198}$	$\substack{1.516 \\ (1.381; 1.650)}$	$\underset{(1.334;1.622)}{1.478}$	$\underset{(1.321;1.676)}{1.476}$	$\substack{1.074 \\ (0.907; 1.241)}$
$\rho_2$	$0.000 \ (-8.224; 8.224)$	-0.207 $(-0.373; -0.042)$	-0.553 $(-0.687; -0.418)$	-0.493 $(-0.636; -0.350)$	-0.485 $(-0.697; -0.327)$	-0.099 $(-0.263;0.067)$
$\sigma_m$	$\substack{0.059 \\ (0.009; 0.195)}$	$0.008 \atop (0.007; 0.009)$	0.007 $(0.007; 0.008)$	$0.009 \atop (0.008; 0.010)$	$\underset{(0.015;0.019)}{0.016}$	$\underset{(0.012;0.015)}{0.013}$
$\delta_0$	$0.000 \ (-8.224; 8.224)$	$\underset{(-0.001;0.001)}{0.000}$	$0.001 \atop (-0.001; 0.003)$	$0.000 \ (-0.002; 0.003)$	$0.001 \atop (-0.004; 0.009)$	$0.001 \atop (-0.001; 0.003)$
$\delta_1$	$0.000 \ (-8.224; 8.224)$	$\underset{(0.842;1.322)}{1.100}$	$0.867 \atop (0.591; 1.112)$	$0.584 \ (0.297; 0.848)$	$0.677 \\ (0.365; 0.949)$	$0.865 \atop (0.650; 1.068)$
$\delta_2$	$0.000 \ (-8.224; 8.224)$	-0.148 $(-0.367;0.102)$	$ \begin{array}{c} 0.041 \\ (-0.186; 0.287) \end{array} $	0.242 $(0.013; 0.475)$	$0.196 \ (-0.068; 0.482)$	$0.094 \ (-0.106; 0.304)$
$\sigma_n$	$\underset{(0.009;0.195)}{0.059}$	$0.006 \atop (0.005; 0.008)$	$\underset{(0.009;0.019)}{0.012}$	$0.021 \atop (0.014; 0.037)$	$\underset{(0.025;0.144)}{0.037}$	$\underset{(0.010;0.016)}{0.012}$

Note: The first column reports the medians for the marginal prior distributions; the other columns provide the analogous statistics for the posterior marginal distributions in each country; numbers in parentheses correspond to the  $5^{\rm th}$  and  $95^{\rm th}$  percentiles.

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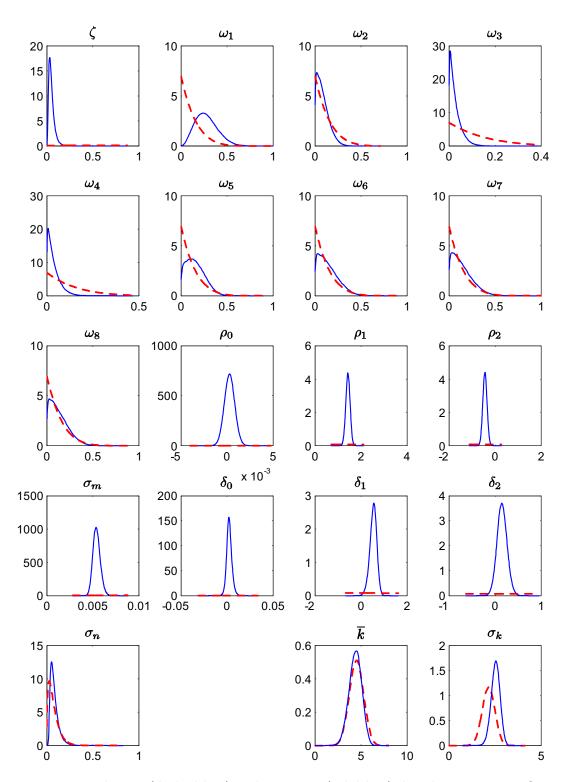


Figure 1: Marginal prior (dashed line) and posterior (solid line) distributions, K=8, flat prior

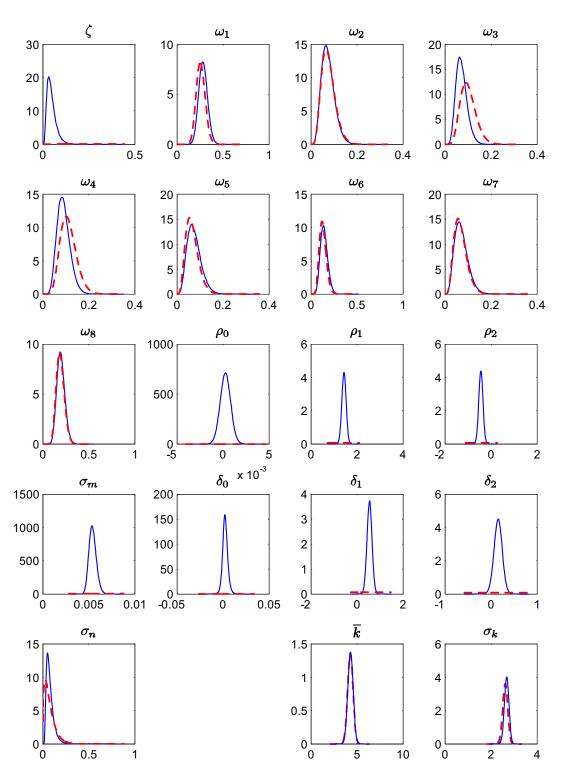


Figure 2: Marginal prior (dashed line) and posterior (solid line) distributions, K=8, informative prior

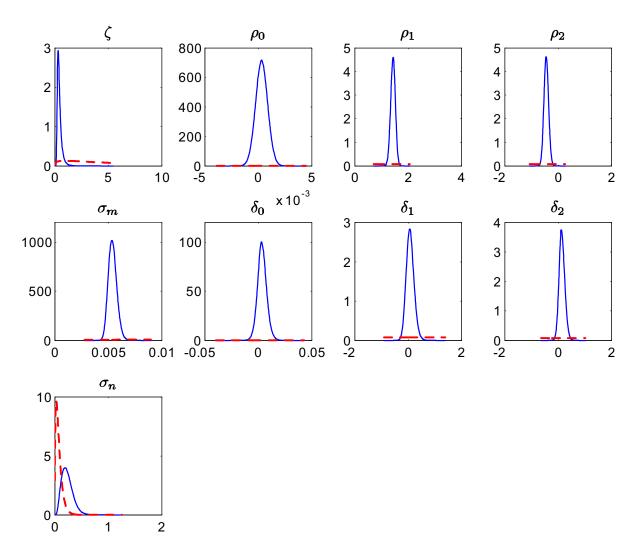


Figure 3: Marginal prior (dashed line) and posterior (solid line) distributions, one-sector model with 7-quarter price spells

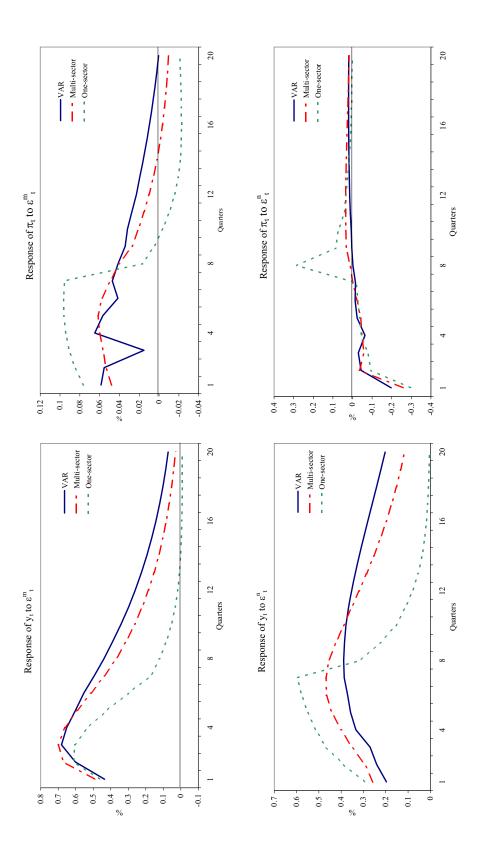


Figure 4: Impulse response functions of models and bivariate VAR